Manual for SIENA version 4.0

Provisional version

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Abstract

SIENA (for Simulation Investigation for Empirical Network Analysis) is a computer program that carries out the statistical estimation of models for the evolution of social networks according to the dynamic actor-oriented model of Snijders (2001, 2005) and Snijders, Steglich, and Schweinberger (2007). This is the manual for SIENA version 4, which is a contributed package to the statistical system R. The manual is based on the earlier manual for SIENA version 3, and also contains contributions written for that manual by Mark Huisman, Michael Schweinberger, and Christian Steglich.

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1 General information

SIENA[1], shorthand for Simulation Investigation for Empirical Network Analysis, is a computer program that carries out the statistical estimation of models for repeated measures of social networks according to the dynamic actor-oriented model of Snijders and van Duijn (1997), Snijders (2001), and Snijders, Steglich, and Schweinberger (2007); also see Steglich, Snijders, and Pearson (2010). A tutorial for these models is in Snijders, van de Bunt, and Steglich (2010). Some examples are presented, e.g., in van de Bunt (1999); van de Bunt, van Duijn, and Snijders (1999); and van Duijn, Zeggelink, Stokman, and Wasseur (2003); and Steglich, Snijders, and West (2006).

A website for SIENA is maintained at `http://www.stats.ox.ac.uk/~snijders/siena/` . At this website ('publications' tab) you shall also find references to introductions in various other languages.

This is a provisional manual for SIENA version 4.0, which is also called RSiena. This is a contributed package for the R statistical system which can be downloaded from `http://cran.r-project.org`. For the operation of R, the reader is referred to the corresponding manual. If desired, SIENA can be operated *apparently* independently of R, as is explained in Section 2.1.

Sometimes latest versions are available at `http://r-forge.r-project.org/R/?group_id=461` before being incorporated into the R package that can be downloaded from CRAN.

RSiena was programmed by Ruth Ripley and Krists Boitmanis, in collaboration with Tom Snijders.

This manual is updated rather frequently, and it may be worthwhile to check now and then for updates. It is possible that the current version still bears some traces from the conversion of SIENA version 3 to 4, and has (mistakenly) some remarks that apply to version 3 and not to 4.

We are grateful to NIH (National Institutes of Health) for their funding of programming RSiena. This is done as part of the project *Adolescent Peer Social Network Dynamics and Problem Behavior*, funded by NIH (Grant Number 1R01HD052887-01A2), Principal Investigator John M. Light (Oregon Research Institute).

For earlier work on SIENA, we are grateful to NWO (Netherlands Organisation for Scientific Research) for their support to the integrated research program *The dynamics of networks and behavior* (project number 401-01-550), the project *Statistical methods for the joint development of individual behavior and peer networks* (project number 575-28-012), the project *An open software system for the statistical analysis of social networks* (project number 405-20-20), and to the foundation ProGAMMA, which all contributed to the work on SIENA.

[1]This program was first presented at the International Conference for Computer Simulation and the Social Sciences, Cortona (Italy), September 1997, which originally was scheduled to be held in Siena. See Snijders & van Duijn (1997).

Part I
Minimal Intro

The following is a minimal cookbook-style introduction for getting started with SIENA using the graphical user interface (*gui*) siena.exe. Later sections explain other ways to run SIENA. If you are looking for help with a specific problem, read the section 2.14.

2 Getting started with SIENA

2.1 Installation and running the graphical user interface under Windows

1. Install R (version 2.9.0 or later). Note that if this leads to any problems or questions, R has an extensive list of 'frequently asked questions' which may contain adequate help for you.
   Start R, click on Packages and then on Install packages(s).... You will be prompted to select a mirror for download. Then select the packages xtable, network, rlecuyer, snow, and RSiena. (There may be later zipped version of RSiena available on our web site: to install this, use Install package(s) from local zip files, and select RSiena.zip (with the appropriate version number in the file name).
   If you are using Windows Vista and get an error of denied permission when trying to install the packages, you may get around this by right-clicking the R icon and selecting 'Run as administrator'.

2. If you want to get the latest beta version of RSiena, before installing the packages, select Packages/Select repositories... and select R-forge. Then install the packages in the normal way.
   Note: On Windows if you select R-forge, by default, CRAN will be removed. On Linux or Mac, by default, both will be selected. Ensure that CRAN is deselected.

3. Install the program siena.exe by, within R, loading the package RSiena using the Packages/Load package... menu. Then, still within R, type installGui(). This will launch the installer which will create shortcuts and Start menu entries for siena.exe. You can then close R.

4. On Linux or Mac, it may be necessary to use
   install.packages("RSiena", repos="http://www.stats.ox.ac.uk/pub/RWin")
   or, for to get the version from R-forge,
   install.packages("RSiena", repos="http://R-Forge.R-project.org")

5. Run siena.exe from the menu or by (double-)clicking a shortcut on the taskbar (or desktop). If this does not work for some reason, then see item number 8 below or consult Section 2.3.

6. In Windows, by right-clicking the shortcut and clicking 'Properties' you can change the current working directory, given in the 'Start in' field. Data files will be searched in first instance in this directory.

7. You should see a screen like that shown in Figure 1

8. If you do not see this screen, navigate in MyComputer to your R distribution (probably somewhere like c:/Program Files/R/R-2.9.0), then move to the bin folder and double click on RSetReg.exe.

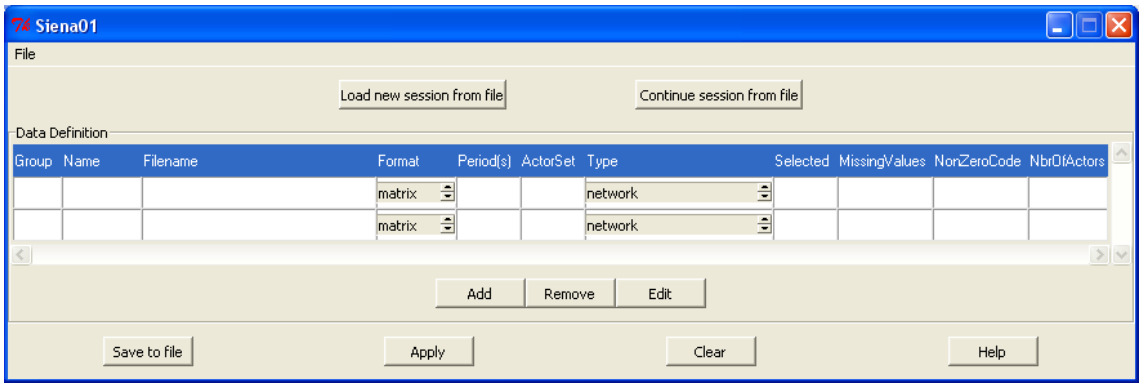


Figure 1: Siena Data Entry Screen

9. Then try running siena again.

10. If the initial screen appears correctly, then check your working directory or folder. This is the directory that is opened immediately when clicking the Add button. Various problems can be avoided by making sure that the working directory is the directory that also contains the data files and the saved session file (see below)!
    You need to have permission to write files in the working directory, and the data files you want to use need to be in the same directory. To do this:

    (a) Right click on the shortcut, and select Properties. (if somehow you don't have permission to do this, try copying the shortcut and pasting to create another with fewer restrictions.) In the Start in: field type the name of the directory in which you wish to work, i.e., a directory in which you can both read and write files. Then click OK.

    (b) To run the examples, put the session file and the two data files in the chosen directory before starting siena.

    (c) To use your own data, put that data in the chosen directory before starting siena.

2.2 Using the graphical user interface from Mac or Linux

1. Install R (version 2.9.0 or greater) as appropriate for your computer.

2. Within R, type
   `install.packages("RSiena")`
   To use the latest beta version, use
   `install.packages("RSiena", repos="http://R-Forge.R-project.org")`

3. Navigate to the directory RSiena package, (which you can find from within R by running `system.file(package="RSiena")`) and find a file called `sienascript`. Run this to produce the Siena GUI screen.(You will probably have to change the permissions first (e.g. `chmod u+x sienascript`)).

4. If you want to use the GUI, you need tcl/tk installed. This is an (optional) part of the R installation on Mac. On Linux, you may need to install Tcl/tk and the extra Tcl/tk package `tktable`. On Ubuntu Linux, the following commands will do what is necessary:[2]

[2]Thanks to Michael Schweinberger and Krists Boitmanis for supplying these.

```
sudo apt-get install tk8.5
sudo apt-get install libtktable2.9
```

2.3 Running the graphical user interface from within R

The GUI interface can be just as easily be executed from within R, which may be helpful if for some reason siena.exe does not operate as desired.[3] This is done by starting up R and working with the following commands. Note that R is case-sensitive, so you must use upper and lower case letters as indicated.

First, set the 'working directory' of the R session to the same directory that holds the data files; for example,
setwd('C:/SienaTest')
(Note the forward slash [4], and the quotes are necessary [5].) Windows users can use the Change dir... option on the File menu.

You can use the following commands to make sure the working directory is what you intend and see which files are included in it:
getwd()
list.files()

Assuming you see the data files, then you can proceed to load the RSiena package, with the library function:
library(RSiena)
The other packages will be loaded as required, but if you wish to examine them or use other facilities from them you can load them using:
library(snow)
library(network)
library(rlecuyer)
The following command will give a review of the functions that RSiena offers:
library(help=RSiena)
After that, you can use the RSiena GUI. It will 'launch' out of the R session.
siena01Gui()
You can monitor the R window for error messages – sometimes they are informative.

When you are done, quit R in the polite way:
q()
(Windows users may quit from the File menu or by closing the window.)

2.4 Entering Data.

There are two ways to enter the data.

1. Enter each of your data files using Add.
   Fill in the various columns as described in Section 2.6.

2. If you have earlier saved the specification of data files, e.g., using Save to file, then you can use Load new session from File.
   This requires a file in the format described at the end of Section 2.6; such a file can be created and read in an editor or spreadsheet program, and it is created in .csv (comma separated) format by the siena01Gui() when you request Save to file.

[3] We are grateful to Paul Johnson for supplying these ideas.
[4] You can use backward ones but they must be doubled: setwd('C:\\SienaTest').
[5] Single or double, as long as they match.

Once you have done this, check that the Format, Period, Type, etc., are correct, and enter any values which indicate missingness in the Missing Values column. A (minimal) complete screen is shown in Figure 2. The details of this screen are explained in Section 2.6.

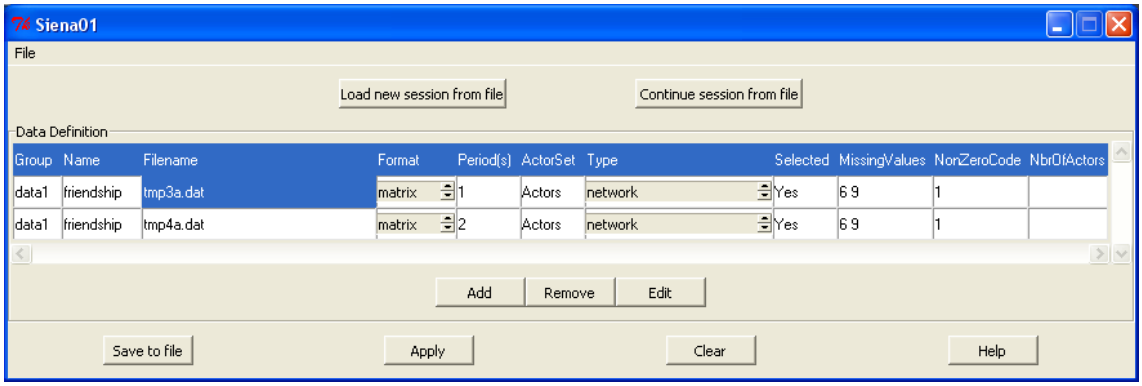


Figure 2: Example of a Completed Data Entry Screen

2.5 Running the Estimation Program

1. Click Apply: you will be prompted to save your work. Then you should see the Model Options screen shown in Figure 3. If this does not happen, then one possible source of error is that

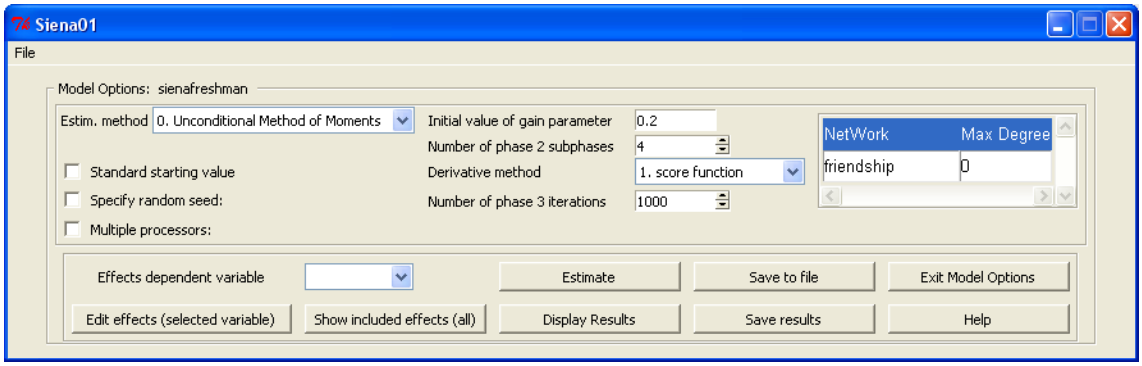


Figure 3: Model options screen

the program cannot find your files; e.g., the files are not in the working directory (see above) but in a different directory.
If errors occur at this moment and the options screen does not appear, then you can obtain diagnostic error messages working not through the siena01Gui, but directly within R as described in Section 2.9.1. This will hopefully help you solving this problem; later on you can then work through the siena01Gui again.

2. Select the options you require.

3. Use Edit Effects to choose the effects you wish to include. Note you can edit the effects for just one dependent variable at a time if you wish by selecting one dependent variable in 'Effects dependent variable'.

4. Click Estimate.

5. You should see the SIENA screen of the estimation program.

6. When the program has finished, you should see the results. If not, click Display Results to see the results. The output file which you will see is stored, with extension `.out` in the directory in which you start siena.exe.

7. You may restart your estimation session at a later date using the Continue session from file on the Data Entry Screen.
   The restart needs a saved version of the data, effects and model as R objects. This will be created automatically when you first enter the Model Options Screen, using the default effects and model. You may save the current version at any time using the Save to file button, and will be prompted to do so when you leave this screen.

2.6 Details of The Data Entry Screen

Group May be left blank unless you wish to use the multi-group option described in Section 12.1. Should not contain embedded blanks.

Name Network files or dyadic covariates should use the same name for each file of the set. Other files should have unique names, a list of space separated ones for constant covariates.

File Name Usually entered by using a file selection box, after clicking Add.

Format Only relevant for networks or dyadic covariates. Can be a matrix; a single Pajek network (.net) (not for two-mode networks); or a Siena network file (an edgelist, containing three or four columns: (from, to, value, wave (optional)), not yet tested for dyadic covariates!).

Period(s) Only relevant for networks and dyadic covariates. All other files cover all the relevant periods. Indicates the order of the network and dyadic covariate files. Should range from 1 to M within each group, where M is the number of time points (waves). Use multiple numbers separated by spaces for multi-wave Siena network files.

ActorSet If you have more than one set of nodes, use this column to indicate which is relevant to each file. Should not contain embedded blanks.

Type Indicate here what type of data the file contains. Options are:

network (i.e., a one-mode network)

bipartite (i.e., a two-mode network)

behavior

constant covariate

changing covariate

constant dyadic covariate

changing dyadic covariate

exogenous event (for changing composition of the actor set)

Selected Yes or No. Only files with Yes will be included in the model.

Missing Values Enter any values which indicate missingness, with spaces between different entries.

Nonzero Codes Enter any values which indicate ties, with spaces between different entries.

NbrOfActors For Siena network files, enter the number of actors. For Siena net bipartite files, enter the two dimensions (number of rows, number of columns) of the network, separated by a blank space.

The details of the screen can be saved to a *session* file, from which they can be reloaded. But you can create a session file directly: it should have columns with exactly the same names and in exactly the same order as those of the Data Entry screen, and be of any of the following types:

Extension	Type
`.csv`	Comma separated
`.dat` or `.prn`	Space delimited
`.txt`	Tab delimited

The root name of this input file will also be the root name of the output file.

2.7 Data formats

1. Network and covariate files should be text files with a row for each node. The numbers should be separated by spaces or tabs.

2. An exogenous events file can be given, indicating change of composition of the network in the sense that some actors are not part of the network during all the observations. This will trigger treatment of such change of composition according to Huisman and Snijders (2003). This file must have one row for each node. Each row should be consist of a set of pairs of numbers which indicate the periods during which the corresponding actor was present. For example,

   ```
   1 3
   1.5 3
   1 1.4 2.3 3
   2.4 3
   ```

   would describe a network with 4 nodes, and 3 observations. Actor 1 is present all the time, actor 2 joins at time 1.5, actor 3 leaves and time 1.4 then rejoins at time 2.3, actor 4 joins at time 2.4. All intervals are treated as closed.

2.8 Continuing the estimation

1. Below you will see some points about how to evaluate the reliability of the results. If the convergence of the algorithm is not quite satisfactory but not extremely poor, then you can continue just by Applying the estimation algorithm again.

2. If the parameter estimates obtained are very poor (not in a reasonable range), then it usually is best to start again, with a simpler model, and from a standardized starting value. The latter option must be selected in the Model Options screen.

2.9 Using SIENA within R

There are two alternatives, depending on your familiarity with R.

Section 2.9.3 presents an example of an R script for getting started with RSiena.

2.9.1 For those who are slightly familiar with R

1. Install R.
2. Install (within R) the package RSiena, and possibly network (required to read Pajek files), snow and rlecuyer (required to use multiple processors).
3. Set the working directory of R appropriately (setwd() within Ror via a desktop shortcut).
4. You can get help by the command

   ```
   help(RSiena)
   ```

   In R version 2.10 this will open a browser window with help information; by clicking on the 'Index' link in the bottom line of this window, you get a window with all RSiena commands. The command

   ```
   RShowDoc("s_man400", package="RSiena")
   ```

   opens the official RSiena manual.
5. Create a session file using siena01Gui() within R, or using an external program.
6. Then, within R,
   (a) Use sienaDataCreateFromSession() to create your data objects.
   (b) Use getEffects() to create an effects object.
   (c) Use fix() to edit the effects object and select the required effects, by altering the Include column to TRUE.
   (d) Use sienaModelCreate() to create a model object.
   (e) Use siena07() to run the estimation procedure.

   Basic output will be written to a file. Further output can be obtained by using the verbose=TRUE option of siena07.

2.9.2 For those fully conversant with R

1. Add the package RSiena
2. Get your network data (including dyadic covariates) into matrices, or sparse matrices of type dgTMatrix. spMatrix() (in package Matrix) is useful to create the latter.
3. Covariate data should be in vectors or matrices.
4. All missing data should be set to NA.
5. Create SIENA objects for each network, behavior variable and covariate, using the functions sienaNet() (for both networks and behavior variables), coCovar() etc.

6. Create a SIENA data object using SienaDataCreate().
7. Use getEffects() to create an effects object.
8. Use fix() to edit the effects object and select the required effects. Alternatively use normal R commands to change the effects object: it is just a data frame.
9. Use sienaModelCreate() to create a model object.
10. Use siena07() to run the estimation procedure.
11. Note that it is possible to use multiple processes in siena07. For details see section 2.11.
12. Also note the availability of the parameter prevAns to reuse estimates and derivatives from a previous run with the same effects.

Basic output will be written to a file. Further output can be obtained by using the verbose=TRUE option of siena07.

2.9.3 An example R script for getting started

The following is an example R script, which one may use to get started with RSiena.

```
#####################################GENERAL#################################

# This is an R script for getting started with RSiena, written by
# Robin Gauthier, Tom Snijders, and Ruth Ripley.
# Lines starting with # are not processed by R but treated as comments.

# R is case sensitive.

# Help within R can be called by typing a question mark and the name of the
# function you need help with. For example ?library loading will bring up a
# file titled "loading and listing of packages".
# Comments are made at the end of commands, or in lines staring with # telling
# R to ignore everything beyond it.
# This session will be using s50 data which are supposed to be
# present in the working directory.
# Note that any command in R is called a function;
# in general the command syntax for calling R's functions is function(x) where
# function is a saved function and x the name of the object to be operated on.

####################CALLING THE DATA AND PRELIMINARY MANIPULATIONS#############

# The library command loads the packages needed during the session.

        library(RSiena)
        library(snow) # (these three additional libraries will be loaded
        library(network)# automatically if required)
        library(rlecuyer)
        library(xtable)

# Where are you?
```

```
        getwd()

# By something like setwd('C:/SienaTest') you can set the directory
# but note the quotes and forward slash. Also possible to set the directory
# using the menus if you have them.

# What is there?

        list.files()

# What is available in RSiena?

        ?RSiena

# Where is the manual?

        RShowDoc("s_man400", package="RSiena")

# (Note, however, that it is possible that the Siena website
# at http://www.stats.ox.ac.uk/~snijders/siena/ contains a more recent version.)

# The data is named (for example I name it friend.data.w1) so that we can call
# it as an object within R.
# If you read an object straight into R, it will treat it as a
# dataset, which is not what we want because it will generally be harder to work
# with than a matrix (unless you want it to be a dataset (i.e. non-network data).
# R will read in many data formats, these are saved as .dat files, the command
# to read them is read.table if we wished to read a .csv file we would have
# used the read.csv command.
# The pathnames have forward slashes, or double backslashes
# if single backslashes are used, one of the error messages will be:
#   1: '\R' is an unrecognized escape in a character string


        friend.data.w1 <- as.matrix(read.table("s50-network1.dat"))
        friend.data.w2 <- as.matrix(read.table("s50-network2.dat"))
        drink <- as.matrix(read.table("s50-alcohol.dat"))

# Before we work with the data, we want to be sure it is correct. A simple way
# to check that our data is a matrix is the command class()

        class(friend.data.w1)

# To check that all the data has been read in, we can use the dim() command. The
# matrix should have the same dimensions as the original data (here, 50 by 50).

        dim(friend.data.w1)

# To check the values are correct, including missing values, we can use
```

```
        table(friend.data.w1, useNA='always')

# We do the same for the changing covariate that I have labelled "drink". Unlike
# the two matrices it should be 50 by 3 because there are three time points in
# the data, although we will only work with two (we are only working with
# two adjacency matrices.

        dim(drink)

# to create NA's, use eg:

        friend.data.w1[friend.data.w1 %in% c(6,9)] <- NA

####################FROM VECTORS AND MATRICES TO SIENA OBJECTS##################

# A number of objects need to be created in R, as preparations to letting Siena07
# execute the estimation.
# sienaModelCreate creates a control object which can be used as an argument for Siena07
# You can look in the RSiena help files, requested by typing ?RSiena,
# to find out about options that you may use here;
# for beginning users, only the two options mentioned below are relevant.
#
# Output will be written to a file with name projname.out, where projname is
# whatever name is given; the default (used if no name is given) is Siena.
# This file will be written to your current directory.
# New estimation runs will append to it.
# A new call to print01Report will overwrite it!

        mymodel <- sienaModelCreate(useStdInits = TRUE, projname = 's50_2')

# sienaNet creates a Siena network object from a matrix or array or list of sparse
# matrix of triples.
# The name of this network object (here: friendship) will be used
# in the output file.
        friendship <- sienaNet(array(c(friend.data.w1, friend.data.w2), dim=c(50, 50, 2)))
# the integers in the dim() here refer to the number of nodes (senders,
# receivers) and the number of waves.
#
# sienaNet is also used to create a behavior variable object
# with the extra argument type="behavior"
# e.g  using the drinking behavior matrix
        alcohol <- sienaNet(drink, type="behavior")
# (but only use the variable once: behavior variable or changing covariate!)

# To create bipartite network objects you need two nodesets and must create
# the node sets too eg:

        friendship <- sienaNet(array(c(friend.data.w1, friend.data.w2),
                                dim=c(50, 50, 2)), nodeSet=c("senders", "receivers"))
```

```
        senders <- sienaNodeSet(50, nodeSetName="senders")
        receivers <- sienaNodeSet(50, nodeSetName="receivers")
        mydata <- sienaDataCreate(friendship, alcohol,
        nodeSets=list(senders, receivers))

# varCovar creates a changing covariate object from a matrix;
# the name comes from 'varying covariate'. We are only using
# two waves of data, so we only want drinking behavior at time 1 and 2, the
# first two columns of the data. The brackets slice the data into the first two
# columns while the comma indicates that R should read all of the rows.
# Omitting the [,1:2] will lead to the same result, as
# RSiena drops an unnecessary final column automatically.
# The name (alcohol) again will be used in the output file.


        alcohol <- varCovar(val = drink[,1:2])

# sienaDataCreate creates a Siena data object from input networks,
# covariates and composition change objects.

        mydata <- sienaDataCreate(friendship,alcohol)

# If you would like to use different names, you could request this as follows:
        mydata <- sienaDataCreate(nominations = friendship, drinking = alcohol)

# This finishes the data specification. Now we have to specify the model.

# getEffects creates a dataframe of effects

        myeff <- getEffects(mydata)

# A basic report of data input, which serves as a check and also contains
# a number of descriptives, can be obtained as follows.
# It produces a file named 'modelname.out' in the current working directory.

        print01Report(mydata,myeff, modelname = 's50_2_init')

# fix calls a data editor, so we can manually edit the effects as in the Gui

        fix(myeff)

# fix() may not be usable if you do not have tcl/tk available

# Alternatively we can edit the dataframe directly by using R functions.
# Note that the columns of the dataframe of effects have names indicated
# in the top of the dataframe:
# name, effectName, type, include, fix, test, initialValue, parm,
# effectnumber, effect1, effect2, effect3.
# The commands below are used to set "include" to TRUE or FALSE,
```

```
# as an alternative to using the data editor.
# TRUE or FALSE will always be located at the 9th column,
# transitive triplets will not always be at the 11th row as this depends
# on the number of periods; further, the list of available effects
# may change in future versions.
# In general the advantage of this method is
# that we can save the last parameters and rerun the model
# later without opening the editor. (Saving can now be done in the GUI).
# Note: These row numbers may not be the current ones, as they depend on the
# list of effects implemented, which is changeable.

        #myeff[11,9] <- TRUE   #transitive triples
        #myeff[15,9] <- TRUE   #3 cycles
        #myeff[17,9] <- TRUE   #transitive ties
        #myeff[27,9] <- TRUE   #indegree popularity
        #myeff[31,9] <- TRUE   #outdegree popularity
        #myeff[34,9] <- TRUE   #indegree based activity
        #myeff[36,9] <- TRUE   #outdegree based activity
        #myeff[46,9] <- TRUE   #indegree-indegree assortativity
        #myeff[48,9] <- TRUE   #alcohol alter
        #myeff[50,9] <- TRUE   #alcohol alter (squared)
        #myeff[52,9] <- TRUE   #alcohol ego
        #myeff[54,9] <- TRUE   #alcohol similarity
        #myeff[62,9] <- TRUE   #alcohol ego x alcohol alter

# Alternatively, and more robustly against future changes in the structure,
# use the following for the last effect:

        #myeff[myeff$effectName=='alcohol ego x alcohol alter' &
        #myeff$type=='eval', 'include']=TRUE)

# and similarly for the earlier ones.
# To specify an interaction between say alcohol and reciprocity,
# where 69 is the row number of an unspecified interaction effect,
# and 52 and 9 are now used as the numbers of the effects
# that get the roles of effect1 and effect2,
# meaning that they are to be interacted, the following can be used;
# the name will be created by siena07.

        #myeff[69, c('effect1', 'effect2')] <- c(52, 9)
        #myeff[69, 'include'] <- TRUE


# new, more robust, methods to amend an effects object:

        #myeff <- includeEffects(myeff, transTrip, cycle3, between)
        #myeff <- includeInteraction(myeff, egoX, recip,
        #   interaction1="alcohol")
        #myeff <- setParameter(myeff, outInv, 3)
```

```
# There is a table of short names etc available as pdf via

        #RShowDoc("effects", package="RSiena")

# or as html by running the function

        #effectsDocumentation()

# siena07 actually fits the specified model to the data

        ans <- siena07(mymodel, data=mydata, effects=myeff, batch=FALSE, verbose=TRUE)

# By using various different effects objects, you can switch between specifications.
# The batch=FALSE parameters will give a graphical user interface being opened;
# verbose=TRUE leads to diagnostic information being sent to the console
# during the estimation, and results after the estimation
# (these results are also copied to the output file projname.out, mentioned above);
# while batch=TRUE gives only a limited amount of printout sent to the console
# during the estimation (which is seen when clicking in the console,
# or more immediately if the Buffered Output is deselected in the Misc menu)
# which helps monitor the progress of the estimation.

# To use multiple processors, in the simplest case where your computer has 2
# processors, use
         ans <- siena07(mymodel, data=mydata, effects=myeff, batch=FALSE,
                        verbose=TRUE, nbrNodes=2, useCluster=TRUE, initC=TRUE)

# Adjust the nbrNodes to the number available. If you wish to use other machines
# as well, see the more detailed instructions below. You will need to use the
# clusterString argument as well.
#
# If you wish the fitted object to include the simulated networks, use the
# parameter returnDeps=TRUE. The fitted object will then have a component named
# sims which will contain a list (each iteration) of lists (each data object)
# of lists (each dependent network or behavior variable) of edgelists for
# networks or vectors for behavior variables.
#
# This option would require rather a lot of communication between multiple
# processes so it might be better to avoid using the two options together.
#
################################################################################

# Depending on the random seed, the results could be something like the following.

#Rates and standard errors

#1 rate basic rate parameter friendship      7.19745  (   1.46778 )
#2 eval outdegree (density)                 -1.64754  (   0.21366 )
#3 eval reciprocity                          2.09008  (   0.38726 )
#4 eval transitive triplets                  0.27810  (   0.16612 )
```

```
#5 eval 3-cycles                              0.50407  (   0.37948 )
#6 eval transitive ties                       0.63643  (   0.23843 )
#7 eval indegree - popularity                 0.04709  (   0.02693 )
#8 eval outdegree - popularity               -0.26251  (   0.66212 )
#9 eval indegree - activity                  -0.17380  (   0.01324 )
#10 eval outdegree - activity                -0.06880  (   0.06258 )
#11 eval in-in degree^(1/2) assortativity     0.03142  (   0.90979 )
#12 eval alcohol alter                       -0.08973  (   0.13641 )
#13 eval alcohol ego                          0.03142  (   0.10044 )
#14 eval alcohol similarity                   1.10065  (   0.72948 )

# With function siena07 we made ans as the object containing
# all the results of the estimation. For example,

        ans$theta

# contains the vector of parameter estimates while

        ans$covtheta

# contains the covariance matrix of the estimates.
# There are several 'methods' available for the object containing the results of
# the estimation.

        ans

# will produce a short table.

        summary(ans)

# will produce a longer report, and

        xtable(ans)

# will produce a table formatted for inclusion in a LaTeX document
# or formatted in html. Use e.g.

        xtable(ans, type='html')

# to get html, and e.g.

        xtable(ans, file='ff.tex')

# to write the results to a file.

# The option useStdInits = TRUE, used above in sienaModelCreate, will make
# each estimation run start with standard initial values.
# If you wish to start the next estimation with the results
# produced by the previous estimation, first change this option:
```

```
        mymodel$useStdInits <- FALSE

# and then initialise the next estimation by the current results.
# If you used unconditional estimation (as here was the default), then request:

        myeff$initialValue[myeff$include] <- ans$theta

# and if you used conditional estimation, conditional on the first network:
        myeff$initialValue[myeff$include] <- c(ans$rate, ans$theta)

# By using a different vector instead of ans$theta you can
# initialise differently.
# Note that this initial vector will be used until you change it again,
# e.g., to the results of a new run,
# or until you change the useStdInits option.

# You can use the prevAns= option in siena07 to supply the result of a
# previous run from which to extract the theta estimates and the
derivatives. Phase 1 will be omitted in this case.

########################VIEWING THE NETWORK IN R########################

# We can make connections with other R packages, e.g., Carter Butts's
# sna (Social Network Analysis) package.
# This package is documented in
# Carter T. Butts, Social Network Analysis with sna,
# Journal of Statistical Software Vol. 24, Issue 6, May 2008
# http://www.jstatsoft.org/v24/i06
# Also see,
# Carter T. Butts, network: A Package for Managing Relational Data in R
# Journal of Statistical Software Vol. 24, Issue 2, May 2008
# http://www.jstatsoft.org/v24/i02
# Here we demonstrate the use of sna for plotting.

        library(sna)

# First we must make the data available in a network format for plotting.
# The function as.network will convert a matrix to a network object.

# NB this command needs the network package loaded (library(network))
net1 <- as.network(friend.data.w1)

# The command plot will visualize the network for you according to the defaults

        plot(net1)

# The plot function is part of the network package, and you can find the
# documentation by requesting ?network and then looking for plot.network
# or ?plot.network
```

```
# Now the same for the second network to the network at the second time period:

        net2 <- as.network(friend.data.w2)
        plot(net2)

# You might try to add the parameter  interactive=TRUE
# which will allow to change vertex positions in the plot.

# We can also color nodes by attributes
# First we must add the node values to the network.
# The %v% operator, documented in the ?network help files, does this.

        net1 %v% "drink1" <- drink[,1]
        net2 %v% "drink2" <- drink[,2]

# Now we can color the node by alcohol attribute.
# In addition we make the arrowheads and nodes a bit larger.

        plot(net1, vertex.col="drink1", object.scale = 0.012, arrowhead.cex=1.1)
        plot(net2, vertex.col="drink2", object.scale = 0.012, arrowhead.cex=1.1)

# Each value of the discrete value of the covariate drink is given a different
# color and we can see if there are clear trends toward homophily in either
# time point.

# We can see that in time one there is one girl holding the groups together,
# and we may wish to know which respondent she is.
# This command simply pulls the id from the nodes in the network:

        plot(net1,label=network.vertex.names(net1), boxed.labels=FALSE)

# If you do not like the place where the labels are put, look in the help file
# at labels.pos and try label.pos = 1, 2, 3, 4, or 5.

# If we want to know how much she drinks, we'll put the commands together:

        plot(net1,vertex.col="drink1",label=network.vertex.names(net1),
             boxed.labels=FALSE, object.scale = 0.012)

# for the network at time two

        plot(net2,vertex.col="drink2",label=network.vertex.names(net2))

# Each time we make a plot the coordinates move - because always
# the starting values are random. We can also save coordinates
# and use them for later plotting:

        coordin1 <- plot(net1, vertex.col="drink1", object.scale = 0.012, arrowhead.cex=1.1)
        plot(net2, coord = coordin1, vertex.col="drink2", object.scale = 0.012, arrowhead.cex=1.1
```

```
# The second plot is not so nice as the first - not surprisingly.
# Another option is to determine the coordinates from both networks together.
# See the "Value" entry in the help file of plot in package network.

        net12 <- net1 + net2
        coordin12 <- plot(net12)
        plot(net1, coord = coordin12, vertex.col="drink1", object.scale = 0.012, arrowhead.cex=1.
        plot(net2, coord = coordin12, vertex.col="drink2", object.scale = 0.012, arrowhead.cex=1.

# There are many other functions in sna that may be useful.
# The following is an example: see the documentation mentioned above for more.
# evcent is the Bonacich eigenvector centrality.

        triad.census(net1)
        betweenness(net1)
        evcent(net1)
```

2.10 Outline of estimation procedure

SIENA estimates parameters by the following procedure:

1. Certain statistics are chosen that should reflect the parameter values;
   the finally obtained parameters should be such that the *expected values* of the statistics are equal to the *observed values*.
   Expected values are approximated as the averages over a lot of simulated networks.
   Observed values are calculated from the data set. These are also called the *target values*.

2. To find these parameter values, an *iterative stochastic simulation algorithm* is applied.
   This works as follows:

   (a) In Phase 1, the sensitivity of the statistics to the parameters is roughly determined.

   (b) In Phase 2, provisional parameter values are updated:
   this is done by simulating a network according to the provisional parameter values, calculating the statistics and the deviations between these simulated statistics and the *target values*, and making a little change (the 'update') in the parameter values that hopefully goes into the right direction.
   (Only a 'hopefully' good update is possible, because the simulated network is only a random draw from the distribution of networks, and not the expected value itself.)

   (c) In Phase 3, the final result of Phase 2 is used, and it is checked if the average statistics of many simulated networks are indeed close to the target values. This is reflected in the so-called `t statistics for deviations from targets`.

2.11 Using multiple processes

1. If multiple processors are available, then using multiple processes can speed up the estimation in siena07.

2. In Phases 1 and 3 the simulations are performed in parallel. In Phase 2, multiple simulations are done with the same parameters, and the resulting statistics are averaged. The gain parameter is increased and the minimum numb er of iterations in phase 2 reduced to take advantage of the increased accuracy.

3. The parameters required to run all processes on one computer are fairly simple: in your call to siena07, set nbrNodes to the number of processes and useCluster and initC to TRUE. The Model Options screen also allows you to specify the number of processors, and will automatically set the other required parameters for you.

4. To use more than one machine is more complicated, but it can be done by using, in addition, the clusterString parameter. The computers need to be running incoming ssh.

5. For machines with exactly the same layout of R directories on each, simply set clusterString to a character vector of the names of the machines.

6. For other cases, e.g. using Macs alongside Linux, see the documentation for the package snow.

7. Currently RSiena uses sockets for inter-process communication.

8. Each process needs a copy of the data in memory. If there is insuffient memory available there will be no speed gain as too much time will be spent paging.

9. In each iteration the main process waits until all the other processes have finished. The overall speed is therefore that of the slowest process, and there should be enough processors to allow them all to run at speed.

2.12 Steps for looking at results: Executing SIENA.

1. Look at the start of the output file for general data description (degrees, etc.), to check your data input.

2. When parameters have been estimated, first look at the `t ratios for deviations from targets`. These are good if they are all smaller than 0.1 in absolute value, and reasonably good if they are all smaller than 0.2.
   We say that the algorithm has converged if they are all smaller than 0.1 in absolute value, and that it has nearly converged if they are all smaller than 0.2.
   These bounds are indications only, and may be taken with a grain of salt.

3. The Initial value of gain parameter determines the step sizes in the parameter updates in the iterative algorithm. A too low value implies that it takes very long to attain a reasonable parameter estimate when starting from an initial parameter value that is far from the 'true' parameter estimate. A too high value implies that the algorithm will be unstable, and may be thrown off course into a region of unreasonable (e.g., hopelessly large) parameter values. It usually is unnecessary to change this.

4. If all this is of no avail, then the conclusion may be that the model specification is incorrect for the given data set.

5. Further help in interpreting output is in Section 6.2 of this manual.

2.13 Giving references

When using SIENA, it is appreciated that you refer to this manual and to one or more relevant references of the methods implemented in the program. The reference to this manual is the following.

Ripley, Ruth M., and Snijders, Tom A.B. 2010. Manual for SIENA version 4.0 (provisional version, January 31, 2010). Oxford: University of Oxford, Department of Statistics; Nuffield College. http://www.stats.ox.ac.uk/siena/

A basic reference for the network dynamics model is Snijders (2001) or Snijders (2005). Basic references for the model of network-behavior co-evolution are Snijders, Steglich, and Schweinberger (2007) and Steglich, Snijders, and Pearson (2010).

More specific references are Schweinberger (2005) for the score-type goodness of fit tests and Schweinberger and Snijders (2007) for the calculation of standard errors of the Method of Moments estimators .

A tutorial is Snijders, van de Bunt, and Steglich (2010).

2.14 Getting help with problems

If you have a problem running RSiena, please read through the following hints to see if any of them help. If not, please send an email to rsiena-help@lists.r-forge.r-project.org, or post in the help forum for RSiena in R-forge. You need to be a registered member of R-forge (and possibly of RSiena) to post to a forum, but anyone can send emails (at present!). In your message, please tell us which operating system , which version of R, and which version of RSiena you are using.

For queries about the modelling aspects of SIENA, or interpretation, please continue to use the StOCNET / RSiena mailing list.

Check your version of RSiena Details of the latest version available can be found at `http://r-forge.r-project.org/R/?group_id=461`. The version is identified by a version number (e.g. 1.0.9) and an R-forge revision number. You can find both the numbers of your current installed version by opening R , and typing `packageDescription("RSiena")`. The version is near the top, the revision number near the end. Both are also displayed at the start of SIENA output files (use print01Report to get the relevant output file if you are not using the gui.)

Check your version of R When there is a new version or revision of RSiena it will only be available to you automatically if you are running the most recent major version of R, currently 2.10. (You can force an installation if necessary by downloading the tarball or binary and installing from that, but it is better to update your R.)

Check both repositories We have two repositories in use for RSiena: CRAN and R-forge. The latest version will always be available from R-forge. (Frequent updates are discouraged on CRAN, so bug-fixes are likely to appear first on R-forge.)

Installation When using the repository at R-forge, *install* the package rather than updating it. Then check the version and revision numbers.

Part II
User's manual

3 Parts of the program

The operation of the SIENA program is comprised of four main parts:

1. input of basic data description,
2. model specification,
3. estimation of parameter values using stochastic simulation,
4. simulation of the model with given and fixed parameter values.

The normal operation is to start with data input, then specify a model and estimate its parameters, and then continue with new model specifications followed by estimation or simulation. For the comparison of (nested) models, statistical tests can be carried out.

The main output is written to a text file named *pname*.out, where *pname* is the root name of the file specifying the data files (if any).

4 Input data

The main statistical method implemented in SIENA is for the analysis of repeated measures of social networks, and requires network data collected at two or more time points. It is possible to include changing actor variables (representing behavior, attitudes, outcomes, etc.) which also develop in a dynamic process, together with the social networks. As repeated measures data on social networks, at the very least, *two or more data files with digraphs* are required: the observed networks, one for each time point. The number of time points is denoted M.

In addition, various kinds of variables are allowed:

1. *actor-bound* or *individual variables*, also called *actor attributes*, which can be symbolized as v_i for each actor i; these can be constant over time or changing;
   the changing individual variables can be dependent variables (changing dynamically in mutual dependence with the changing network) or independent variables (exogenously changing variables; then they are also called individual covariates).

2. *dyadic covariates*, which can be symbolized as w_{ij} for each ordered pair of actors (i, j); these likewise can be constant over time or changing.

All variables must be available in ASCII ('raw text') data files, described in detail below. It is best to use the 'classical' type of filenames, without embedded blanks and not containing special characters. These files, the names of the corresponding variables, and the coding of missing data, must be made available to SIENA.

Names of variables must be composed of at most 12 characters. This is because they are used as parts of the names of effects which can be included in the model, and the effect names should not be too long.

4.1 Digraph data files

Each digraph must be contained in a separate input file. Two data formats are allowed currently. For large number of nodes (say, larger than 100), the Pajek format is preferable to the adjacency matrix format. For more than a few hundred nodes,

1. *Adjacency matrices.*
   The first is an adjacency matrix, i.e., n lines each with n integer numbers, separated by blanks or tabs, each line ended by a hard return. The diagonal values are meaningless but must be present.

   Although this section talks only about digraphs (directed graphs), it is also possible that all observed adjacency matrices are symmetric. This will be automatically detected by SIENA, and the program will then utilize methods for non-directed networks.

   The data matrices for the digraphs must be coded in the sense that their values are converted by the program to the 0 and 1 entries in the adjacency matrix. A set of code numbers is required for each digraph data matrix; these codes are regarded as the numbers representing a present arc in the digraph, i.e., a 1 entry in the adjacency matrix; all other numbers will be regarded as 0 entries in the adjacency matrix. Of course, there must be at least one such code number. All code numbers must be in the range from 0 to 9, except for structurally determined values (see below).

   This implies that if the data are already in 0-1 format, the single code number 1 must be given. As another example, if the data matrix contains values 1 to 5 and only the values 4 and 5 are to be interpreted as present arcs, then the code numbers 4 and 5 must be given.

2. *Pajek format.*
   If the digraph data file has extension name `.net`, then the program assumes that the data file has Pajek format. The format required differs from that in the previous versions of SIENA . The file should relate to one observation only, and should contain a list of vertices (using the keyword `*Vertices`, together with (currently) a list of arcs, using the keyword `*Arcs` followed by data lines according to the Pajek rules. These keywords must be in lines that contain no further characters. An example of such input files is given in the s50 data set that is distributed in the `examples` directory.

3. *Siena format.*
   An edge list containing three or four columns: from, to, value, wave (optional).
   Like the Pajek format, this has the advantage that absent ties (tie variables with the value 0) do not need to be mentioned in the data file.

Code numbers for missing numbers also must be indicated – in the case of either input data format. These codes must, of course, be different from the code numbers representing present arcs.

Although this section talks only about digraphs (directed graphs), it is also possible that all observed ties (for all time points) are mutual. This will be automatically detected by SIENA, and the program will then utilize methods for non-directed networks.

If the data set is such that it is never observed that ties are terminated, then the network dynamics is automatically specified internally in such a way that termination of ties is impossible. (In other words, in the simulations of the actor-based model the actors have only the option to create new ties or to retain the status quo, not to delete existing ties.)

4.1.1 Structurally determined values

It is allowed that some of the values in the digraph are structurally determined, i.e., deterministic rather than random. This is analogous to the phenomenon of 'structural zeros' in contingency tables, but in SIENA not only structural zeros but also structural ones are allowed. A structural zero means that it is certain that there is no tie from actor i to actor j; a structural one means that it is certain that there is a tie. This can be, e.g., because the tie is impossible or formally imposed, respectively.

Structural zeros provide an easy way to deal with actors leaving or joining the network between the start and the end of the observations. Another way (more complicated but it gives possibilities to represent actors entering or leaving at specified moments between observations) is described in Section 4.7.

Structurally determined values are defined by reserved codes in the input data: the value 10 indicates a structural zero, the value 11 indicates a structural one. Structurally determined values can be different for the different time points. (The diagonal of the data matrix always is composed of structural zeros, but this does not have to be indicated in the data matrix by special codes.) The correct definition of the structurally determined values can be checked from the brief report of this in the output file.

Structural zeros offer the possibility of analyzing several networks simultaneously under the assumption that the parameters are identical. Another option to do this is given in Section 12. E.g., if there are three networks with 12, 20 and 15 actors, respectively, then these can be integrated into one network of $12 + 20 + 15 = 47$ actors, by specifying that ties between actors in different networks are structurally impossible. This means that the three adjacency matrices are combined in one 47×47 data file, with values 10 for all entries that refer to the tie from an actor in one network to an actor in a different network. In other words, the adjacency matrices will be composed of three diagonal blocks, and the off-diagonal blocks will have all entries equal to 10. In this example, the number of actors per network (12 to 20) is rather small to obtain good parameter estimates,

but if the additional assumption of identical parameter values for the three networks is reasonable, then the combined analysis may give good estimates.

In such a case where K networks (in the preceding paragraph, the example had $K = 3$) are combined artificially into one bigger network, it will often be helpful to define $K - 1$ dummy variables at the actor level to distinguish between the K components. These dummy variables can be given effects in the rate function and in the evaluation function (for "ego"), which then will represent that the rate of change and the out-degree effect are different between the components, while all other parameters are the same.

It will be automatically discovered by SIENA when functions depend only on these components defined by structural zeros, between which tie values are not allowed. For such variables, only the ego effects are defined and not the other effects defined for the regular actor covariates and described in Section 5.3. This is because the other effects then are meaningless. If at least one case is missing (i.e., has the missing value data code for this covariate), then the other covariate effects are made available.

When SIENA simulates networks including some structurally determined values, if these values are constant across all observations then the simulated tie values are likewise constant. If the structural fixation varies over time, the situation is more complicated. Consider the case of two consecutive observations m and $m + 1$, and let X_{ij}^{sim} be the simulated value at the end of the period from t_m to t_{m+1}. If the tie variable X_{ij} is structurally fixed at time t_m at a value $x_{ij}(t_m)$, then X_{ij}^{sim} also is equal to $x_{ij}(t_m)$, independently of whether this tie variable is structurally fixed at time t_{m+1} at the same or a different value or not at all. This is the direct consequence of the structural fixation. On the other hand, the following rule is also used. If X_{ij} is *not* structurally fixed at time t_m but it is structurally fixed at time t_{m+1} at some value $x_{ij}(t_{m+1})$, then in the course of the simulation process from t_m to t_{m+1} this tie variable can be changed as part of the process in the usual way, but after the simulation is over and before the statistics are calculated it will be fixed to the value $x_{ij}(t_{m+1})$.

The target values for the algorithm of the Method of Moments estimation procedure are calculated for all observed digraphs $x(t_{m+1})$. However, for tie variables X_{ij} that are structurally fixed at time t_m, the observed value $x_{ij}(t_{m+1})$ is replaced by the structurally fixed value $x_{ij}(t_m)$. This gives the best possible correspondence between target values and simulated values in the case of changing structural fixation.

4.2 Dyadic covariates

As the digraph data, also each measurement of a dyadic covariate must be contained in a separate input file with a square data matrix, i.e., n lines each with n integer numbers, separated by blanks or tabs, each line ended by a hard return. The diagonal values are meaningless but must be present. Pajek input format is currently not possible for dyadic covariates.

A distinction is made between constant and changing dyadic covariates, where change refers to changes over time. Each constant covariate has one value for each pair of actors, which is valid for all observation moments, and has the role of an independent variable. Changing covariates, on the other hand, have one such value for each period between measurement points. If there are M waves of network data, this covers $M - 1$ periods, and accordingly, for specifying a single changing dyadic covariate, $M - 1$ data files with covariate matrices are needed.

The mean is always subtracted from the covariates. See the section on *Centering*.

4.3 Individual covariates

Individual (i.e., actor-bound) variables can be combined in one or more files. If there are k variables in one file, then this data file must contain n lines, with on each line k numbers which all are read

as real numbers (i.e., a decimal point is allowed). The numbers in the file must be separated by blanks and each line must be ended by a hard return. There must not be blank lines after the last data line.

Also here, a distinction is made between constant and changing actor variables. Each constant actor covariate has one value per actor valid for all observation moments, and has the role of an independent variable.

Changing variables can change between observation moments. They can have the role of dependent variables (changing dynamically in mutual dependence with the changing network) or of independent variables; in the latter case, they are also called 'changing individual covariates'. Dependent variables are treated in the section below, this section is about individual variables in the role of independent variables – then they are also called individual covariates.

When changing individual variables have the role of independent variables, they are assumed to have constant values from one observation moment to the next. If observation moments for the network are $t_1, t_2, ..., t_M$, then the changing covariates should refer to the $M-1$ moments t_1 through t_{M-1}, and the m-th value of the changing covariates is assumed to be valid for the period from moment t_m to moment t_{m+1}. The value at t_M, the last moment, does not play a role. Changing covariates, as independent variables, are meaningful only if there are 3 or more observation moments, because for 2 observation moments the distinction between constant and changing covariates is not meaningful.

Each changing individual covariate must be given in one file, containing $k = M-1$ columns that correspond to the $M-1$ periods between observations. It is not a problem if there is an M'th column in the file, but it will not be read.

The mean is always subtracted from the covariates. See the section on *Centering*.

When an actor covariate is constant within waves, or constant within components separated by structural zeros (which means that ties between such components are not allowed), then only the ego effect of the actor covariate is made available. This is because the other effects then are meaningless. This may cause problems for combining several data sets in a meta-analysis (see Section 12). If at least one case is missing (i.e., has the missing value data code), then the other covariate effects are made available. When analysing multiple data sets in parallel, for which the same set of effects is desired to be included it is therefore advisable to give data sets in which a given covariate has the same value for all actors one missing value in this covariate; purely to make the total list of effects independent of the observed data.

4.4 Interactions and dyadic transformations of covariates

For actor covariates, two kinds of transformations to dyadic covariates are made internally in SIENA. Denote the actor covariate by v_i, and the two actors in the dyad by i and j. Suppose that the range of v_i (i.e., the difference between the highest and the lowest values) is given by r_V. The two transformations are the following:

1. *dyadic similarity*, defined by $1-\left(|v_i-v_j|/r_V\right)$, and centered so the the mean of this similarity variable becomes 0;
   note that before centering, the similarity variable is 1 if the two actors have the same value, and 0 if one has the highest and the other the lowest possible value;

2. *same* V, defined by 1 if $v_i = v_j$, and 0 otherwise (not centered) (V is the name of the variable). This can also be referred to as *dyadic identity* with respect to V.

Dyadic similarity is relevant for variables that can be treated as interval-level variables; dyadic identity is relevant for categorical variables.

In addition, SIENA offers the possibility of user-defined two- and three-variable interactions between covariates; see Section 5.5.

4.5 Dependent action variables

SIENA also allows dependent action variables, also called dependent behavior variables. This can be used in studies of the co-evolution of networks and behavior, as described in Snijders, Steglich, and Schweinberger (2007) and Steglich, Snijders, and Pearson (2010). These action variables represent the actors' behavior, attitudes, beliefs, etc. The difference between dependent action variables and changing actor covariates is that the latter change exogenously, i.e., according to mechanisms not included in the model, while the dependent action variables change endogenously, i.e., depending on their own values and on the changing network. In the current implementation only one dependent network variable is allowed, but the number of dependent action variable can be larger than one. Unlike the changing individual covariates, the values of dependent action variables are not assumed to be constant between observations.

Dependent action variables must have nonnegative integer values; e.g., 0 and 1, or a range of integers like 0,1,2 or 1,2,3,4,5. Each dependent action variable must be given in one file, containing $k = M$ columns, corresponding to the M observation moments.

If any values are not integers, a warning will be printed on the initial report and the values will be truncated towards zero.

4.6 Missing data

SIENA allows that there are some missing data on network variables, on covariates, and on dependent action variables. Missing data in changing dyadic covariates are not yet implemented. Missing data must be indicated by missing data codes, *not* by blanks in the data set.

Missingness of data is treated as non-informative. One should be aware that having many missing data can seriously impair the analyses: technically, because estimation will be less stable; substantively, because the assumption of non-informative missingness often is not quite justified. Up to 10% missing data will usually not give many difficulties or distortions, provided missingness is indeed non-informative. When one has more than 20% missing data on any variable, however, one may expect problems in getting good estimates.

In the current implementation of SIENA, missing data are treated in a simple way, trying to minimize their influence on the estimation results. This method is further explained in Huisman and Steglich (2008), where comparisons are also made with other ways of dealings with the missing information.

The basic idea is the following. A brief sketch of the procedure is that missing values are imputed to allow meaningful simulations; for the calculation of the target statistics in the Method of Moments, tie variables and actor variables with missings are not used. More in detail, the procedure is as follows.

The simulations are carried out over all variables, as if they were complete. To enable this, missing data are imputed. In the initial observation, missing entries in the adjacency matrix are set to 0, i.e., it is assumed that there is *no* tie; this is done because normally data are sparse, so 'no tie' is the modal value of the tie variable. In the further observations, for any variable, if there is an earlier observed value of this variable then the last observed value is used to impute the current value (the 'last observation carry forward' option, cf. Lepkowski, 1989); if there is no earlier observed value, the value 0 is imputed. For the dependent behavior variables the same principle is used: if there is a previous observation of the same variable then this value is imputed, if there is none then the observationwise mode of the variable is imputed. Missing covariate data are replaced by the variable's average score at this observation moment. In the course of the simulations, however, the adjusted values of the dependent action variables and of the network variables are allowed to change.

In order to ensure a minimal impact of missing data treatment on the results of parameter

estimation (method of moments estimation) and/or simulation runs, the calculation of the target statistics used for these procedures uses only non-missing data. When for an actor in a given period, any variable is missing that is required for calculating a contribution to such a statistic, this actor in this period does not contribute to the statistic in question. For network and dependent action variables, the tie variable or the actor variable, respectively, must provide valid data both at the beginning and at the end of a period for being counted in the respective target statistics.

4.7 Composition change

SIENA can also be used to analyze networks of which the composition changes over time, because actors join or leave the network between the observations. This can be done in two ways: using the method of Huisman and Snijders (2003), or using structural zeros. (For the maximum likelihood estimation option, the Huisman-Snijders method is not implemented, and only the structural zeros method can be used.) Structural zeros can specified for all elements of the tie variables toward and from actors who are absent at a given observation moment. How to do this is described in subsection 4.1.1. This is straightforward and not further explained here. This subsection explains the method of Huisman and Snijders (2003), which uses the information about composition change in a sightly more efficient way.

For this case, a data file is needed in which the *times of composition change* are given. For networks with constant composition (no entering or leaving actors), this file is omitted and the current subsection can be disregarded.

Network composition change, due to actors joining or leaving the network, is handled separately from the treatment of missing data. The digraph data files must contain all actors who are part of the network at any observation time (denoted by n) and each actor must be given a separate (and fixed) line in these files, even for observation times where the actor is not a part of the network (e.g., when the actor did not yet join or the actor already left the network). In other words, the adjacency matrix for each observation time has dimensions $n \times n$.

At these times, where the actor is not in the network, the entries of the adjacency matrix can be specified in two ways. First as missing values using missing value code(s). In the estimation procedure, these missing values of the joiners before they joined the network are regarded as 0 entries, and the missing entries of the leavers after they left the network are fixed at the last observed values. This is different from the regular missing data treatment. Note that in the initial data description the missing values of the joiners and leavers are treated as regular missing observations. This will increase the fractions of missing data and influence the initial values of the density parameter.

A second way is by giving the entries a regular observed code, representing the absence or presence of an arc in the digraph (as if the actor was a part of the network). In this case, additional information on relations between joiners and other actors in the network before joining, or leavers and other actors after leaving can be used if available. Note that this second option of specifying entries always supersedes the first specification: if a valid code number is specified this will always be used.

For joiners and leavers, crucial information is contained in the times they join or leave the network (i.e., the times of composition change), which must be presented in a separate input file, the *exogenous events file* described in Section 2.7.

4.8 Centering

Individual as well as dyadic covariates are centered by the program in the following way.

For individual covariates, the mean value is subtracted immediately after reading the variables. For the changing covariates, this is the global mean (averaged over all periods). The values of

these subtracted means are reported in the output.

For the dyadic covariates and the similarity variables derived from the individual covariates, the grand mean is calculated, stored, and subtracted during the program calculations. (Thus, dyadic covariates are treated by the program differently than individual covariates in the sense that the mean is subtracted at a different moment, but the effect is exactly the same.)

The formula for balance is a kind of dissimilarity between rows of the adjacency matrix. The mean dissimilarity is subtracted in this formula and also reported in the output. This mean dissimilarity is calculated by a formula given in Section 13.

5 Model specification

After defining the data, the next step is to specify a model.

The model specification consists of a selection of 'effects' for the evolution of each dependent variable (network or behavior).

For the longitudinal case, three types of effects are distinguished (see Snijders, 2001; Snijders, van de Bunt, and Steglich, 2010):

- *rate function effects*
  The rate function models the speed by which the dependent variable changes; more precisely: the speed by which each network actor gets an opportunity for changing her score on the dependent variable.
  Advice: in most cases, start modeling with a constant rate function without additional rate function effects. Constant rate functions are selected by exclusively checking the 'basic rate parameter' (for network evolution) and the main rate effects (for behavioral evolution) on the model specification screen. (When there are important size or activity differences between actors, it is possible that different advice must be given, and it may be necessary to let the rate function depend on the individual covariate that indicates this size; or on the out-degree.)

- *evaluation function effects*
  The evaluation function[6] models the network actors' satisfaction with their local network neighborhood configuration. It is assumed that actors change their scores on the dependent variable such that they improve their total satisfaction – with a random element to represent the limited predictability of behavior. In contrast to the endowment function (described below), the evaluation function evaluates only the local network neighborhood configuration that results from the change under consideration. In most applications, the evaluation function will be the main focus of model selection.
  The network evaluation function normally should always contain the 'density', or 'out-degree' effect, to account for the observed density. For directed networks, it mostly is also advisable to include the reciprocity effect, this being one of the most fundamental network effects. Likewise, behavior evaluation functions should normally always contain the shape parameter, to account for the observed prevalence of the behavior, and (unless the behavior is dichotomous) the quadratic shape effect, to account more precisely for the distribution of the behavior.

- *endowment function effects*
  The endowment function[7] is an extension of the evaluation function that allows to distinguish between new and old network ties (when evaluating possible network changes) and between increasing or decreasing behavioral scores (when evaluating possible behavioral changes). The function models the loss of satisfaction incurred when existing network ties are dissolved or when behavioral scores are decreased to a lower value (hence the label 'endowment').
  For a number of effects, the endowment function is implemented not for the Method of Moments estimation method, but only for Maximum Likelihood and Bayesian estimation. This is indicated in Section 13.
  Advice: start modeling without any endowment effects, and add them at a later stage. Do not use endowment effects for behavior unless the behavior variable is dichotomous.

The estimation and simulation procedures of SIENA operate on the basis of the model specification which comprises the set of effects included in the model as described above, together with

[6] The evaluation function was called *objective function* in Snijders, 2001.
[7] The endowment function is similar to the *gratification function* in Snijders, 2001.

the current parameter values. After data input, the constant rate parameters and the density effect in the network evaluation function have default initial values, depending on the data. All other parameter values initially are 0. The estimation process changes the current value of the parameters to the estimated values. Values of effects not included in the model are not changed by the estimation process. It is possible for the user to change parameter values and to request that some of the parameters are fixed in the estimation process at their current value.

5.1 Important structural effects for network dynamics: one-mode networks

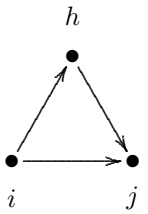
For the structural part of the model for network dynamics, for one-mode (or unipartite) networks, the most important effects are as follows. The mathematical formulae for these and other effects are given in Section 13. Here we give a more qualitative description.

A default model choice could consist of (1) the out-degree and reciprocity effects; (2) one network closure effect, e.g. transitive triplets or transitive ties; the 3-cycles effect; (3) the in-degree popularity effect (raw or square root version); the out-degree activity effect (raw or square root version); and either the in-degree activity effect or the out-degree popularity effect (raw or square root function). The two effects (1) are so basic they cannot be left out. The two effects selected under (2) represent the dynamics in local (triadic) structure; and the three effects selected under (3) represent the dynamics in in- and out-degrees (the first for the dispersion of in-degrees, the second for the dispersion of out-degrees, and the third for the covariance between in- and out-degrees) and also should offer some protection, albeit imperfect, for potential ego- and alter-effects of omitted actor-level variables.

The basic list of these and other effects is as follows.

1. The *out-degree effect* which always must be included.
2. The *reciprocity effect* which practically always must be included.
3. There is a choice of four network closure effects. Usually it will be sufficient to express the tendency to network closure by including one or two of these. They can be selected by theoretical considerations and/or by their empirical statistical significance. Some researchers may find the last effect (distances two) less appealing because it expresses network closure inversely.

   a. The *transitive triplets effect*, which is the classical representation of network closure by the number of transitive triplets. For this effect the contribution of the tie $i \to j$ is proportional to the total number of transitive triplets that it forms – which can be transitive triplets of the type $\{i \to j \to h;\ i \to h\}$ as well as $\{i \to h \to j;\ i \to j\}$;



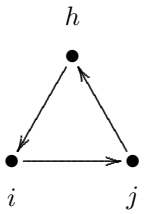
   b. The *balance effect*, which may also be called *structural equivalence with respect to outgoing ties*. This expresses a preference of actors to have ties to those other actors who have a similar set of outgoing ties as themselves. Whereas the transitive triplets effect focuses on how many same choices are made by ego (the focal actor) and alter (the other actor) — the number of h for which $i \to h$ and $j \to h$, i.e., $x_{ih} = x_{jh} = 1$ where i is ego and j is alter — , the balance effect considers in addition how many the same non-choices are made — $x_{ih} = x_{jh} = 0$.

   c. The *transitive ties effect* is similar to the transitive triplets effect, but instead of considering for each other actor j how many two-paths $i \to h \to j$ there are, it is only

considered whether there is at least one such indirect connection. Thus, one indirect tie suffices for the network embeddedness.

d. The *number of actors at distance two effect* expresses network closure inversely: stronger network closure (when the total number of ties is fixed) will lead to fewer geodesic distances equal to 2. When this effect has a negative parameter, actors will have a preference for having few others at a geodesic distance of 2 (given their out-degree, which is the number of others at distance 1); this is one of the ways for expressing network closure.

4. The *three-cycles effect*, which can be regarded as generalized reciprocity (in an exchange interpretation of the network) but also as the opposite of hierarchy (in a partial order interpretation of the network). A negative three-cycles effect, together with a positive transitive triplets or transitive ties effect, may be interpreted as a tendency toward local hierarchy. The three-cycles effect also contributes to network closure.
In a non-directed network, the three-cycles effect is identical to the transitive triplets effect.



5. Another triadic effect is the *betweenness effect*, which represents brokerage: the tendency for actors to position themselves between not directly connected others, i.e., a preference of i for ties $i \rightarrow j$ to those j for which there are many h with $h \rightarrow i$ and $h \not\rightarrow j$.

⊙ The following eight degree-related effects may be important especially for networks where degrees are theoretically important and represent social status or other features important for network dynamics; and/or for networks with high dispersion in in- or out-degrees (which may be an empirical reflection of the theoretical importance of the degrees). Include them if there are theoretical reasons for doing so, but only in such cases.

6. The *in-degree popularity effect* (again, with or without 'sqrt', with the same considerations applying) reflects tendencies to dispersion in in-degrees of the actors; or, tendencies for actors with high in-degrees to attract extra incoming ties 'because' of their high current in-degrees.

7. The *out-degree popularity effect* (again, with or without 'sqrt', with the same considerations applying) reflects tendencies for actors with high out-degrees to attract extra incoming ties 'because' of their high current out-degrees. This leads to a higher correlation between in-degrees and out-degrees.

8. The *in-degree activity effect* (with or without 'sqrt') reflects tendencies for actors with high in-degrees to send out extra outgoing ties 'because' of their high current in-degrees. This leads to a higher correlation between in-degrees and out-degrees. The in-degree popularity and out-degree activity effects are not distinguishable in Method of Moments estimation; then the choice between them must be made on theoretical grounds.

9. The *out-degree activity effect* (with or without 'sqrt') reflects tendencies for actors with high out-degrees to send out extra outgoing ties 'because' of their high current out-degrees. This also leads to dispersion in out-degrees of the actors.

10. The *in-in degree assortativity effect* (where parameter 2 is the same as the sqrt version, while parameter 1 is the non-sqrt version) reflects tendencies for actors with high in-degrees to preferably be tied to other actors with high in-degrees.

11. The *in-out degree assortativity effect* (with parameters 2 or 1 in similar roles) reflects tendencies for actors with high in-degrees to preferably be tied to other actors with high out-degrees.

12. The *out-in degree assortativity effect* (with parameters 2 or 1 in similar roles) reflects tendencies for actors with high out-degrees to preferably be tied to other actors with high in-degrees.

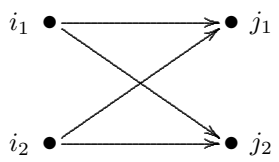
13. The *out-out degree assortativity effect* (with parameters 2 or 1 in similar roles) reflects tendencies for actors with high out-degrees to preferably be tied to other actors with high out-degrees.

5.2 Important structural effects for network dynamics: two-mode networks

For the structural part of the model for network dynamics, for two-mode (or bipartite) networks, the most important effects are as follows. The mathematical formulae for these and other effects are given in Section 13. Here we give a more qualitative description.

1. The *out-degree effect* which always must be included.

2. Transitivity in two-mode networks is expressed in the first place by the number of *four-cycles* (Robins and Alexander, 2005). This reflects the extent to which actors who make one choice in common also make other choices in common.



⊙ The following three degree-related effects may be important especially for networks where degrees are theoretically important and represent social status or other features important for network dynamics; and/or for networks with high dispersion in in- or out-degrees (which may be an empirical reflection of the theoretical importance of the degrees). Include them if there are theoretical reasons for doing so, but only in such cases.

3. The *out-degree activity effect* (with or without 'sqrt'; often the sqrt version, which transforms the degrees in the explanatory role by the square root, works better) reflects tendencies to dispersion in out-degrees of the actors.

4. The *in-degree popularity effect* (again, with or without 'sqrt', with the same considerations applying) reflects tendencies to dispersion in in-degrees of the column units.

5. The *out-in degree assortativity effect* (where parameter 2 is the same as the sqrt version, while parameter 1 is the non-sqrt version) reflects tendencies for actors with high out-degrees to preferably be tied to column units with high in-degrees.

5.3 Effects for network dynamics associated with covariates

For each individual covariate, there are several effects which can be included in a model specification, both in the network evolution part and in the behavioral evolution part (should there be dependent behavior variables in the data). Of course for two-mode networks, the covariates must be compatible with the network with respect to number of units (rows/columns).

- *network rate function*

    1. the covariate's effect on the rate of network change of the actor;

- *network evaluation and endowment functions*

    1. the covariate-similarity effect; a positive parameter implies that actors prefer ties to others with similar values on this variable – thus contributing to the network-autocorrelation of this variable not by changing the variable but by changing the network;
    2. the effect on the actor's activity (covariate-ego); a positive parameter will imply the tendency that actors with higher values on this covariate increase their out-degrees more rapidly;
    3. the effect on the actor's popularity to other actors (covariate-alter); a positive parameter will imply the tendency that the in-degrees of actors with higher values on this covariate increase more rapidly;
    4. the effect of the squared variable on the actor's popularity to other actors (squared covariate-alter) (included only if the range of the variable is at least 2). This normally makes sense only if the covariate-alter effect itself also is included in the model. A negative parameter implies a unimodal preference function with respect to alters' values on this covariate;
    5. the interaction between the value of the covariate of ego and of the other actor (covariate ego $\times$ covariate alter); a positive effect here means, just like a positive similarity effect, that actors with a higher value on the covariate will prefer ties to others who likewise have a relatively high value; when used together with the alter effect of the squared variable this effect is quite analogous to the similarity effect, and for dichotomous covariates, in models where the ego and alter effects are also included, it even is equivalent to the similarity effect (although expressed differently), and then the squared alter effect is superfluous;
    6. the 'same covariate', or covariate identity, effect, which expresses the tendency of the actors to be tied to others with exactly the same value on the covariate; whereas the preceding four effects are appropriate for interval scaled covariates (and mostly also for ordinal variables), the identity effect is suitable for categorical variables;
    7. the interaction effect of covariate-similarity with reciprocity;
    8. the effect of the covariate of those to whom the actor is indirectly connected, i.e., through one intermediary but not with a direct tie; this value-at-a-distance can represent effects of indirectly accessed social capital.

The usual order of importance of these covariate effects on network evolution is: evaluation effects are most important, followed by endowment and rate effects. Inside the group of evaluation effects, it is the covariate-similarity effect that is most important, followed by the effects of covariate-ego and covariate-alter.

When the network dynamics is not smooth over the observation waves — meaning that the pattern of ties created and terminated, as reported in the initial part of the output file under the heading *Initial data description – Change in networks – Tie changes between subsequent observations*, is very irregular across the observation periods — it can be important to include effects of time variables on the network. Time variables are changing actor covariates that depend only on the observation number and not on the actors. E.g., they could be dummy variables, being 1 for one or some observations, and 0 for the other observations.

For actor covariates that are constant within observation waves, or – in the case that there are structurally determined values – constant within connected components, only the ego effects are defined, because only those effects are meaningful. This exclusion of the alter, similarity and other effects for such actor variables applies only to variables without any missing values.

For each dyadic covariate, the following network evaluation effects can be included in the model for network evolution:

- *network evaluation and endowment functions*
  1. main effect of the dyadic covariate;
  2. the interaction effect of the dyadic covariate with reciprocity.

The main evaluation effect is usually the most important. In the current version of SIENA, there are no effects of dyadic covariates on behavioral evolution.

5.4 Effects on behavior evolution

For models with one or more dependent behavior variables, i.e., models for the co-evolution of networks and behavior, the most important effects for the behavior dynamics are the following; see Steglich, Snijders, and Pearson (2010). In these descriptions, with the 'alters' of an actor we refer to the other actors to whom the focal actor has an outgoing tie. The dependent behavior variable is referred to as Z.

1. The shape effect, expressing the basic drive toward high values on Z. A zero value for the shape will imply a drift toward the midpoint of the range of the behavior variable.

2. The effect of the behavior Z on itself, or quadratic shape effect, which is relevant only if the number of behavioral categories is 3 or more. This can be interpreted as giving a quadratic preference function for the behavior. When the coefficient for the shape effect is β_1^Z and for the effect of Z on itself, or quadratic shape effect, is β_2^Z, then the contributions of these two effects are jointly $\beta_1^Z\,(z_i - \bar{z}) + \beta_2^Z\,(z_i - \bar{z})^2$. With a negative coefficient β_2^Z, this is a unimodal preference function, with the maximum attained for $z_i = \bar{z} - 2\,\beta_1^Z/\beta_2^Z$. (Of course additional effects will lead to a different picture; but as long as the additional effects are linear in z_i – which is not the case for similarity effects! –, this will change the location of the maximum but not the unimodal shape of the function.) This can also be regarded as negative feedback, or a self-correcting mechanism: when z_i increases, the further push toward higher values of z_i will become smaller and when z_i decreases, the further push toward lower values of z_i will become smaller. On the other hand, when the coefficient β_2^Z is positive, the feedback will be positive, so that changes in z_i are self-reinforcing. This can be an indication of addictive behavior.

3. The average similarity effect, expressing the preference of actors to being similar with respect to Z to their alters, where the total influence of the alters is the same regardless of the number of alters.

4. The total similarity effect, expressing the preference of actors to being similar to their alters, where the total influence of the alters is proportional to the number of alters.

5. The average alter effect, expressing that actors whose alters have a higher average value of the behavior Z, also have themselves a stronger tendency toward high values on the behavior.

6. The indegree effect, expressing that actors with a higher indegree (more 'popular' actors) have a stronger tendency toward high values on the behavior.

7. The outdegree effect, expressing that actors with a higher outdegree (more 'active' actors) have a stronger tendency toward high values on the behavior.

Effects 1 and 2 will practically always have to be included as control variables. (For dependent behavior variables with 2 categories, this applies only to effect 1.) When the behavior dynamics is not smooth over the observation waves — meaning that the pattern of steps up and down, as reported in the initial part of the output file under the heading *Initial data description – Dependent actor variables – Changes*, is very irregular across the observation periods — it can be important to include effects of time variables on the behavior. Time variables are changing actor covariates that depend only on the observation number and not on the actors. E.g., they could be dummy variables, being 1 for one or some observations, and 0 for the other observations.

The average similarity, total similarity, and average alter effects are different specifications of social influence. The choice between them will be made on theoretical grounds and/or on the basis of statistical significance.

For each actor-dependent covariate as well as for each of the other dependent behavior variables, the effects on Z which can be included is the following.

1. The main effect: a positive value implies that actors with a higher value on the covariate will have a stronger tendency toward high Z values.

2. Interactions between two or three actor variables, see Section 5.5.

5.5 Additional interaction effects

It is possible for the user to define additional interaction effects for the network. The basis is provided by the initial definition, by SIENA, of 'unspecified interaction effects'. Modifying two or three of the columns named 'effect1', 'effect2', and 'effect3' of the effects dataframe allows the definition of two-way or three-way interactions. The *effectNumber* of the effects between which an interaction is required should be entered in the 'effect1' and 'effect2', and for three-way effects, the 'effect3' columns. The interaction effect must also be 'included', but the underlying effects need only be 'included' if they are also required individually.

includeInteraction is an R function provided to facilitate the definition of interaction effects. Such effects can be specified simply by short names and the names of any variables required to identify the underlying effects: it is not necessary to know the effectNumbers of the effects. (The effectNumbers would change if new effects are introduced to RSiena.) Information about short names of effects can be found in the file 'effects.pdf' in the doc directory of the library, accessible from within R using the command

```
RShowDoc("effects", package="RSiena")
```

Alternatively a new version of this list can be displayed in a browser by using the function:

```
effectsDocumentation()
```

5.5.1 Interaction effects for network dynamics

The following kinds of user-defined interactions are possible for the network dynamics.

a. Ego effects of actor variables can interact with all effects.

b. Dyadic effects can interact with each other.

(The column "InteractionType" in the effects data frame indicates which effects are 'ego' effects and which are 'dyadic' effects.)

Thus a two-way interaction must be between two dyadic effects or between one ego effect and another effect. A three-way interaction may be between three dyadic effects, two dyadic effects and an ego effect, or two ego effects and another effect.

All effects used in interactions must be defined on the same network (in the role of dependent variable): that for which the "unspecified interaction effects" is defined. And either all must be evaluation effects or all must be endowment effects.

6 Estimation

The model parameters are estimated under the specification given during the model specification part, using a stochastic approximation algorithm. Only one estimation procedure is currently implemented: the Method of Moments (MoM) (Snijders, 2001; Snijders, Steglich, and Schweinberger, 2007);

In the following, the number of parameters is denoted by p. The algorithm is based on repeated (and repeated, and repeated...) simulation of the evolution process of the network. These repetitions are called 'runs' in the following. The MoM estimation algorithm is based on comparing the observed network (obtained from the data files) to the hypothetical networks generated in the simulations.

Note that the estimation algorithm is of a stochastic nature, so the results can vary! This is of course not what you would like. For well-fitting combinations of data set and model, the estimation results obtained in different trials will be very similar. It is good to repeat the estimation process at least once for the models that are to be reported in papers or presentations, to confirm that what you report is a stable result of the algorithm.

The initial value of the parameters normally is the current value (that is, the value that the parameters have immediately before you start the estimation process); as an alternative, it is possible to start instead with a standard initial value. Usually, a sequence of models can be fitted without problems, each using the previously obtained estimate as the starting point for the new estimation procedure. Sometimes, however, problems may occur during the estimation process, which will be indicated by some kind of warning in the output file or by parameter estimates being outside a reasonably expected range. In such cases the current parameter estimates may be unsatisfactory, and using them as initial values for the new estimation process might again lead to difficulties in estimation. Therefore, when the current parameter values are unlikely and also when they were obtained after a divergent estimation algorithm, it is advisable to start the estimation algorithm with a *standard initial value*. The use of standard initial values is one of the model options. If this has successfully led to a model with convergent parameter estimates and model fitting is continued, then the option can be reset to the current initial values.

6.1 Algorithm

The estimation algorithm is an implementation of the Robbins-Monro (1951) algorithm, described in Snijders (2001, 2002), and has three phases:

1. In phase 1, the parameter vector is held constant at its initial value. This phase is for having a first rough estimate of the matrix of derivatives.

2. Phase 2 consists of several subphases. More subphases means a greater precision. The default number of subphases is 4. The parameter values change from run to run, reflecting the deviations between generated and observed values of the statistics. The changes in the parameter values are smaller in the later subphases.
   The program searches for parameter values where these deviations average out to 0. This is reflected by what is called the 'quasi-autocorrelations' in the output screen. These are averages of products of successively generated deviations between generated and observed statistics. It is a good sign for the convergence of the process when the quasi-autocorrelations are negative (or positive but close to 0), because this means the generated values are jumping around the observed values.

3. In phase 3, the parameter vector is held constant again, now at its final value. This phase is for estimating the covariance matrix and the matrix of derivatives used for the computation

of standard errors.
The default number of runs in phase 3 is 1000. This requires a lot of computing time, but when the number of phase 3 runs is too low, the standard errors computed are rather unreliable.

The number of subphases in phase 2, and the number of runs in phase 3, can be changed in the model options.

The user can break in and modify the estimation process in three ways:

1. it is possible to terminate the estimation;
2. in phase 2, it is possible to terminate phase 2 and continue with phase 3;

6.2 Output

The output file is an ASCII ('text') file which can be read by any text editor. It is called *pname*.out (recall that pname is the project name defined by the user).

The output is divided into sections indicated by a line `@1`, subsections indicated by a line `@2`, subsubsections indicated by `@3`, etc. For getting the main structure of the output, it is convenient to have a look at the `@1` marks first.

The primary information in the output of the estimation process consists of the following three parts. Results are presented here which correspond to Table 2, column "t_1, t_3" of Snijders (2001). The results were obtained in an independent repetition of the estimation for this data set and this model specification; since the repetition was independent, the results are slightly different, illustrating the stochastic nature of the estimation algorithm.

1. Convergence check

In the first place, a convergence check is given, based on Phase 3 of the algorithm. This check considers the deviations between simulated values of the statistics and their observed values (the latter are called the 'targets'). Ideally, these deviations should be 0. Because of the stochastic nature of the algorithm, when the process has properly converged the deviations are small but not exactly equal to 0. The program calculates the averages and standard deviations of the deviations and combines these in a t-ratio (in this case, average divided by standard deviation). For longitudinal modeling, convergence is excellent when these t-ratios are less than 0.1 in absolute value, good when they are less than 0.2, and moderate when they are less than 0.3. For published results, it is suggested that estimates presented come from runs in which all t-ratios for convergence are less than 0.1 in absolute value – or nearly so. (These bounds are indications only, and are not meant as severe limitations.) The corresponding part of the output is the following.

```
Total of 1954 iterations.
Parameter estimates based on 954 iterations,
basic rate parameter as well as
convergence diagnostics, covariance and derivative matrices based on 1000 iterations.

Information for convergence diagnosis.
Averages, standard deviations, and t-ratios for deviations from targets:
  1.     -0.236    7.006   -0.034
  2.      0.204    7.059    0.029
  3.     -1.592   22.242   -0.072

Good convergence is indicated by the t-ratios being close to zero.
```

In this case, the t-ratios are -0.034, -0.029, and -0.072, which is less than 0.1 in absolute value, so the convergence is excellent. In data exploration, if one or more of these t-ratios are larger in

absolute value than 0.3, it is advisable to restart the estimation process. For results that are to be reported, it is advisable to carry out a new estimation when one or more of the t-ratios are larger in absolute value than 0.1. Large values of the averages and standard deviations are in themselves not at all a reason for concern.

For maximum likelihood estimation, the convergence of the algorithm is more problematic than for longitudinal modeling. A sharper value of the t-ratios must be found before the user may be convinced of good convergence. It is advisable to try and obtain t-values which are less than 0.15. If, even with repeated trials, the algorithm does not succeed in producing t-values less than 0.15, then the estimation results are of doubtful value.

2. Parameter values and standard errors

The next crucial part of the output is the list of estimates and standard errors. For this data set and model specification, the following result was obtained.

```
@3
Estimates and standard errors

 0. Rate parameter                              5.4292  (   0.6920)
Other parameters:
 1. eval:  outdegree (density)                 -0.7648  (   0.2957)
 2. eval:  reciprocity                          2.3071  (   0.5319)
 3. eval:  number of actors at distance 2      -0.5923  (   0.1407)
```

The rate parameter is the parameter called ρ in section 13.1.4 below. The value 5.4292 indicates that the estimated number of changes per actor (i.e., changes in the choices made by this actor, as reflected in the row for this actor in the adjacency matrix) between the two observations is 5.43 (rounded in view of the standard error 0.69). Note that this refers to unobserved changes, and that some of these changes may cancel (make a new choice and then withdraw it again), so the average observed number of differences per actor will be somewhat smaller than this estimated number of unobserved changes.

The other three parameters are the weights in the *evaluation function*. The terms in the evaluation function in this model specification are the out-degree effect defined as s_{i1} in Section 13.1.1, the reciprocity effect s_{i2}, and the number of distances 2 (indirect relations) effect, defined as s_{i5}. Therefore the estimated evaluation function here is

$$-0.76\, s_{i1}(x) \;+\; 2.31\, s_{i2}(x) \;-\; 0.59\, s_{i5}(x) \;.$$

The standard errors can be used to test the parameters. For the rate parameter, testing the hypothesis that it is 0 is meaningless because the fact that there are differences between the two observed networks implies that the rate of change must be positive. The weights in the evaluation function can be tested by t-statistics, defined as estimate divided by its standard error. (Do not confuse this t-test with the t-ratio for checking convergence; these are completely different although both are t ratios!) Here the t-values are, respectively, -0.7648/0.2957 = -2.59, 2.3071/0.5319 = 4.34, and -0.5923/0.1407 = -4.21. Since these are larger than 2 in absolute value, all are significant at the 0.05 significance level. It follows that there is evidence that the actors have a preference for reciprocal relations and for networks with a small number of other actors at a distance 2. The value of the density parameter is not very important; it is important that this parameter is included to control for the density in the network, but as all other statistics are correlated with the density, the density is difficult to interpret by itself.

When for some effects the parameter estimate as well as the standard error are quite large, say, when both are more than 2, and certainly when both are more than 5, then it is possible that this indicates poor convergence of the algorithm: in particular, it is possible that the effect in question does have to be included in the model to have a good fit, but the precise parameter value is poorly

defined (hence the large standard error) and the significance of the effect cannot be tested with the t-ratio. This can be explored by estimating the model without this parameter, and also with this parameter fixed at some large value (see section 11.1) – whether the value is large positive or large negative depends on the direction of the effect. For the results of both model fits, it is advisable to check the fit by simulating the resulting model and considering the statistic corresponding to this particular parameter. (The indicative sizes of 2 and 5 result from experience with network effects and with effects of covariates on usual scales with standard deviations ranging between, say, 0.4 and 2. These numbers have to be modified for covariates with different standard errors.)

3. Collinearity check

After the parameter estimates, the covariance matrix of the estimates is presented. In this case it is

```
Covariance matrix of estimates (correlations below diagonal):
     0.087     -0.036      0.003
    -0.230      0.283     -0.033
     0.078     -0.440      0.020
```

The diagonal values are the variances, i.e., the squares of the standard errors (e.g., 0.087 is the square of 0.2957). Below the diagonal are the correlations. E.g., the correlation between the estimated density effect and the estimated reciprocity effect is -0.230. These correlations can be used to see whether there is an important degree of collinearity between the effects. Collinearity means that several different combinations of parameter values could represent the same data pattern, in this case, the same values of the network statistics. When one or more of the correlations are very close to -1.0 or +1.0, this is a sign of near collinearity. This will also lead to large standard errors of those parameters. It is then advisable to omit one of the corresponding effects from the model, because it may be redundant given the other (strongly correlated) effect. It is possible that the standard error of the retained effect becomes much smaller by omitting the other effect, which can also mean a change of the t-test from non-significance to significance.

However, correlations between parameter estimates close to -1.0 or +1.0 should not be used too soon in themselves as reasons to exclude effects from a model. This is for two reasons. In the first place, network statistics often are highly correlated (for example, total number of ties and number of transitive triplets) and these correlations just are one of the properties of networks. Second, near collinearity is not a problem in itself, but the problem (if any) arises when standard errors are high, which may occur because the value of the parameters of highly correlated variables is very hard to estimate with any precision. The problem resides in the large standard errors, not in itself in the strong correlation between the parameter estimates. If for both parameters the ratio of parameter estimate to standard error, i.e., the t-ratio, is larger than 2 in absolute value, in spite of the high correlations between the parameter estimates, then the significance of the t-test is evidence anyway that both effects merit to be included in the model. In other words, in terms of the 'signal-to-noise ratio': the random noise is high but the signal is strong enough that it overcomes the noise.

As a rule of thumb for parameter correlations, usually for correlations of estimated structural network effects there is no reason for concern even when these correlations are as strong as .9.

6.2.1 Fixing parameters

Sometimes an effect must be present in the model, but its precise numerical value is not well-determined. E.g., if the network at time t_2 would contain only reciprocated choices, then the model should contain a large positive reciprocity effect but whether it has the value 3 or 5 or 10 does not make a difference. This will be reflected in the estimation process by a large estimated value and a large standard error, a derivative which is close to 0, and sometimes also by lack of

convergence of the algorithm. (This type of problem also occurs in maximum likelihood estimation for logistic regression and certain other generalized linear models; see Geyer and Thompson (1992, Section 1.6), Albert and Anderson (1984), Hauck and Donner (1978).) In such cases this effect should be fixed to some large value and not left free to be estimated. This can be specified in the model specification under the Edit Effects button. As another example, when the network observations are such that ties are formed but not dissolved (some entries of the adjacency matrix change from 0 to 1, but none or hardly any change from 1 to 0), then it is possible that the density parameter must be fixed at some high positive value.

6.2.2 Automatic fixing of parameters

If the algorithm encounters computational problems, sometimes it tries to solve them automatically by fixing one (or more) of the parameters. This will be noticeable because a parameter is reported in the output as being fixed without your having requested this. This automatic fixing procedure is used, when in phase 1 one of the generated statistics seems to be insensitive to changes in the corresponding parameter.

This is a sign that there is little information in the data about the precise value of this parameter, when considering the neighborhood of the initial parameter values. However, it is possible that the problem is not in the parameter that is being fixed, but is caused by an incorrect starting value of this parameter or one of the other parameters.

When the warning is given that the program automatically fixed one of the parameter, try to find out what is wrong.

In the first place, check that your data were entered correctly and the coding was given correctly, and then re-specify the model or restart the estimation with other (e.g., 0) parameter values. Sometimes starting from different parameter values (e.g., the default values implied by the model option of "standard initial values") will lead to a good result. Sometimes, however, it works better to delete this effect altogether from the model.

It is also possible that the parameter does need to be included in the model but its precise value is not well-determined. Then it is best to give the parameter a large (or strongly negative) value and indeed require it to be fixed (see Section 11.1).

6.2.3 Conditional and unconditional estimation

SIENA has two methods for MoM estimation and simulation: conditional and unconditional. They differ in the *stopping rule* for the simulations of the network evolution. In unconditional estimation, the simulations of the network evolution in each time period (and the co-evolution of the behavioral dimensions, if any are included) carry on until the predetermined time length (chosen as 1.0 for each time period between consecutive observation moments) has elapsed.

In conditional estimation, in each period the simulations run on until a stopping criterion is reached that is calculated from the observed data. Conditioning is possible for each of the dependent variables (network, or behavior), where 'conditional' means 'conditional on the observed number of changes on this dependent variable'.

Conditioning on the network variable means running simulations until the number of different entries between the initially observed network of this period and the simulated network is equal to the number of entries in the adjacency matrix that differ between the initially and the finally observed networks of this period.

Conditioning on a behavioral variable means running simulations until the sum of absolute score differences on the behavioral variable between the initially observed behavior of this period and the simulated behavior is equal to the sum of absolute score differences between the initially and the finally observed behavior of this period.

Conditional estimation is slightly more stable and efficient, because the corresponding rate parameters are not estimated by the Robbins Monro algorithm, so this method decreases the number of parameters estimated by this algorithm. The possibility to choose between unconditional and the different types of conditional estimation is one of the model options.

If there are changes in network composition (see Section 4.7), only the unconditional estimation procedure is available.

6.2.4 Required changes from conditional to unconditional estimation

Even though conditional estimation is slightly more efficient than unconditional estimation, there is one kind of problem that sometimes occurs with conditional estimation and which is not encountered by unconditional estimation.

It is possible (but luckily rare) that the initial parameter values were chosen in an unfortunate way such that the conditional simulation does not succeed in ever attaining the condition required by its stopping rule (see Section 6.2.3). The solution is either to use standard initial values or to to unconditional estimation.

7 Standard errors

The estimation of standard errors of the MoM estimates requires the estimation of derivatives, which indicate how sensitive the expected values of the statistics (see Section 6.1) are with respect to the parameters. The derivatives can be estimated by three methods:

(0) finite differences method with common random numbers,

(1) score function method 1 (default),

(2) score function method 2 (not currently implemented).

Schweinberger and Snijders (2006) point out that the finite differences method is associated with a bias-variance dilemma, and proposed the unbiased and consistent score function methods. These methods demand less computation time than method (0). It is recommended to use at least 1000 iterations (default) in phase 3. For published results, it is recommended to have 2000 or 4000 iterations in phase 3.

8 Tests

Two types of tests are available in SIENA.

1. t-type tests of single parameters can be carried out by dividing the parameter estimate by its standard error. Under the null hypothesis that the parameter is 0, these tests have approximately a standard normal distribution.

2. Score-type tests of single and multiple parameters are described in the following section.

8.1 Score-type tests

A generalized Neyman-Rao score test is implemented for the MoM estimation method in SIENA (see Schweinberger, 2005).

Most goodness-of-fit tests will have the following form: some model is specified and one or more parameters are restricted to some constant, in most cases 0 – these constant values define the null hypothesis being tested. This can be obtained in RSiena by appropriate choices in the effects dataframe (called myeff in Section 2.9.3). Parameters can be restricted by putting 1 in the fix and test columns when editing the effects, and the tested value in the initialValue column. For example, when the effect for which the score test is desired has effectNumber equal to 46, the commands can be as follows.

```
myeff[46,9] <- TRUE
myeff[46, 'fix'] <- TRUE
myeff[46, 'test'] <- TRUE
myeff[46, 'initialValue'] <- ((value to be used for test))
```

The goodness-of-fit test proceeds by simply estimating the restricted model (not the unrestricted model, with unrestricted parameters) by the standard SIENA estimation algorithm. No more information needs to be communicated.

8.2 Example: one-sided tests, two-sided tests, and one-step estimates

Suppose that it is desired to test the goodness-of-fit of the model restricted by the null hypothesis that the reciprocity parameter is zero. The following output may be obtained:

```
@2
Generalised score test <c>
--------------------------

Testing the goodness-of-fit of the model restricted by

 (1)   eval:  reciprocity                                =  0.0000
------------------------------------------------

   c =   3.9982   d.f. = 1   p-value =   0.0455
   one-sided (normal variate):   1.9996
------------------------------------------------

One-step estimates:

1: constant network rate (period 1)                6.3840
```

```
l: constant network rate (period 2)                6.4112
eval:  outdegree (density)                         0.9404
eval:  reciprocity                                 1.2567
```

To understand what test statistic `<c>` is about, consider the case where the network is observed at two time points, and let R be the number of reciprocated ties at the second time point. Then it can be shown that the test statistic is some function of

Expected R under the restricted model $-$ observed R.

Thus, the test statistic has some appealing interpretation in terms of goodness-of-fit: when reciprocated ties do have added value for the firms—which means that the reciprocity parameter is not 0, other than the model assumes—then the deviation of the observed R from the R that is expected under the model will be large (large misfit), and so will be the value of the test statistic. Large values of the test statistic imply low p-values, which, in turn, suggests to abandon the model in favor of models incorporating reciprocity.

The null distribution of the test statistic c tends, as the number of observations increases, to the chi-square distribution, with degrees of freedom equal to the number of restricted parameters. The corresponding p-value is given in the output file.

In the present case, one parameter is restricted (reciprocity), hence there is one degree of freedom `d.f. = 1`. The value of the test statistic `c = 3.9982` at one degree of freedom gives `p = 0.0455`. That is, it seems that reciprocity should be included into the model and estimated as the other parameters.

The one-sided test statistic, which can be regarded as normal variate, equals `1.9996` indicating that the value of the transitivity parameter is positive.

The one-step estimates are approximations of the unrestricted estimates (that is, the estimates that would be obtained if the model were estimated once again, but without restricting the reciprocity parameter). The one-step estimate of reciprocity, `1.2567`, hints that this parameter is positive, which agrees with the one-sided test.

8.2.1 Multi-parameter tests

In the case where $K > 1$ model parameters are restricted, SIENA evaluates the test statistic with K degrees of freedom. A low p-value of the joint test would indicate that the goodness-of-fit of the model is intolerable. However, the joint test with K degrees of freedom gives no clue as to what parameters should be included into the model: the poor goodness-of-fit could be due to only one of the K restricted parameters, it could be due to two of the K restricted parameters, or due to all of them. Hence SIENA carries out, in addition to the joint test with K degrees of freedom, additional tests with one degree of freedom that test the single parameters one-by-one. The goodness-of-fit table looks as follows:

```
@2
Generalised score test <c>
--------------------------

Testing the goodness-of-fit of the model restricted by

 (1)   eval:  covariate_ij (centered)                  =  0.0000
 (2)   eval:  covariate_i alter                        =  0.0000
 (3)   eval:  covariate_i similarity                   =  0.0000
-----------------------------------------------
```

```
Joint test:
-----------
   c =  92.5111   d.f. = 3   p-value [ 0.0001

(1) tested separately:
----------------------
 - two-sided:
   c =  62.5964   d.f. = 1   p-value [ 0.0001
 - one-sided (normal variate):   7.9118

(2) tested separately:
----------------------
 - two-sided:
   c =  16.3001   d.f. = 1   p-value [ 0.0001
 - one-sided (normal variate):   4.0373

(3) tested separately:
----------------------
 - two-sided:
   c =  23.4879   d.f. = 1   p-value [ 0.0001
 - one-sided (normal variate):   4.8464
-------------------------------------------------

One-step estimates:

l: constant network rate (period 1)                7.4022
l: constant network rate (period 2)                6.4681
eval:  outdegree (density)                        -0.4439
eval:  reciprocity                                 1.1826
eval:  transitive triplets                         0.1183
eval:  covariate_ij (centered)                     0.4529
eval:  covariate_i alter                           0.1632
eval:  covariate_i similarity                      0.4147
```

In the example output, three parameters are restricted. The joint test has test statistic c, which has under the null hypothesis a chi-squared distribution with d.f. = 3. The p-value corresponding to the joint test indicates that the restricted model is not tenable. Looking at the separate tests, it seems that the misfit is due to all three parameters. Thus, it is sensible to improve the goodness-of-fit of the baseline model by including all of these parameters, and estimate them.

8.3 Alternative application: convergence problems

An alternative use of the score test statistic is as follows. When convergence of the estimation algorithm is doubtful, it is sensible to restrict the model to be estimated. Either "problematic" or "non-problematic" parameters can be kept constant at preliminary estimates (estimated parameters values). Though such strategies may be doubtful in at least some cases, it may be, in other cases, the only viable option besides simply abandoning "problematic" models. The test statistic can be exploited as a guide in the process of restricting and estimating models, as small values of the test statistic indicate that the imposed restriction on the parameters is not problematic.

8.4 Testing differences between independent groups

Sometimes it is interesting to test differences between parameters estimated for independent groups. For example, for work-related support networks analyzed in two different firms, one might wish to test whether the tendency to reciprocation of work-related support, as reflected by the reciprocity parameter, is equally strong in both firms. Such a comparison is meaningful especially if the total model is the same in both groups, as control for different other effects would compromise the basis of comparison of the parameters.

If the parameter estimates in the two networks are $\hat{\beta}_a$ and $\hat{\beta}_b$, with standard errors $s.e_a$ and $s.e_b$, respectively, then the difference can be tested with the test statistic

$$\frac{\hat{\beta}_a - \hat{\beta}_b}{\sqrt{s.e_a^2 + s.e_b^2}}\ , \tag{1}$$

which under the null hypothesis of equal parameters has an approximating standard normal distribution.

9 Simulation

The simulation option still must be made available in a clear way for SIENA version 4.

The simulation option simulates the network evolution for fixed parameter values. This is meaningful mainly at the point that you have already estimated parameters, and then either want to check again whether the statistics used for estimation have expected values very close to their observed values, or want to compute expected values of other statistics.

The number of runs is set at a default value of 1,000, and can be changed in the simulation options. The user can break in and terminate the simulations early. When only 1 run is requested, an entire data set is generated and written to file in SIENA format and also in Pajek format.

The output file contains means, variances, covariances, and correlations of the selected statistics. The output file also contains t-statistics for the various statistics; these can be regarded as tests for the simple null hypothesis that the model specification with the current parameter values is correct.

For simulating networks and behavior, the output includes the autocorrelation statistics known as Moran's I and Geary's c. For formulae and interpretation see, e.g., Ripley (1981, 98–99). These measure the extent to which the value of the variable in question is similar between tied actors. This similarity is expressed by relatively high values for Moran's I and by relatively low values for Geary's c. The null values, which are the expected values for variables independent of the network, are given by $-1/(n-1)$ for Moran's I and by 1 for Geary's c.

(The output of the descriptive statistics, which can be obtained from Siena02, also contains Moran's I and Geary's c, computed for the observed data, together with their null means and standard deviations.)

The simulation feature can be used in the following way. Specify a model and estimate the parameters. After this estimation (supposing that it converged properly), add a number of potential effects. This number might be too large for the estimation algorithm. Therefore, do not Estimate but choose Simulate instead. The results will indicate which are the statistics for which the largest deviations (as measured by the t-statistics) occurred between simulated and observed values. Now go back to the model specification, and return to the specification for which the parameters were estimated earlier. The effects corresponding to the statistics with large t-values are candidates for now being added to the model. One should be aware, however, that such a data-driven approach leads to capitalization on chance. Since the selected effects were chosen on the basis of the large deviation between observed and expected values, the t-tests, based on the same data set, will tend to give significant results too easily. The tests described in Section 8 do not have this problem of chance capitalization.

The generated statistics for each run are also written to the file *pname*.sdt ('sdt' for 'simulation data'), so you can inspect them also more precisely. This file is overwritten each time you are simulating again. A brief history of what the program does is again written to the file *pname*.log.

9.1 Conditional and unconditional simulation

The distinction between conditional and unconditional simulation is the same for the simulation as for the estimation option of SIENA, described in Section 6.2.3.

If the conditional simulation option was chosen (which is the default) and the simulations do not succeed in achieving the condition required by its stopping rule (see Section 6.2.3), then the simulation is terminated with an error message, saying *This distance is not achieved for this parameter vector*. In this case, you are advised to change to unconditional simulation.

10 Options for model type, estimation and simulation

There are several options available in SIENA. The main options concern the model type and the estimation procedure used.

1. There is a choice between conditional (1) and unconditional (0) Method of Moments estimation. If there are dependent action variables, the default for conditional estimation is to condition on the observed distance for the network variable; but it then is possible also to condition on the distances observed for the dependent action variables.

2. The number of subphases in phase 2 of the estimation algorithm.
   This determines the precision of the estimate. Advice: 3 for quick preliminary investigations, 4 or 5 for serious estimations.

3. The number of runs in phase 3 of the estimation algorithm.
   This determines the precision of the estimated standard errors (and covariance matrix of the estimates), and of the t-values reported as diagnostics of the convergence. Advice: 200 for preliminary investigations when precise standard errors and t-values are not important, 1000 for serious investigations, 2000 to 4000 for estimations of which results are to be reported in publications.
   (These numbers can be twice as low if, instead of the new (from Version 2.3) default option of estimation by the Score Function method, the older method of Finite Differences is used. The latter method has runs that take more time, but needs fewer runs.)

4. The initial gain value, which is the step size in the starting steps of the Robbins-Monro procedure, indicated in Snijders (2001) by a_1 .

5. The choice between standard initial values (suitable estimates for the density and reciprocity parameters and zero values for all other parameters) or the current parameter values as initial values for estimating new parameter values.

6. A random number seed. If the value 0 is chosen, the program will randomly select a seed. This is advised to obtain truly random results. If results from an earlier run are to be exactly replicated, the random number seed from this earlier run can be used.

7. The method to estimate derivatives; 0 is the older finite differences method 1 is the more efficient and unbiased method proposed by Schweinberger and Snijders (2007); this is the preferred method. See Section 7.

There is one option for simulations that can be chosen here.

1. The number of runs in the straight simulations.
   Advice: the default of 1000 will usually be adequate.

Depending on the choice for conditional or unconditional estimation in the estimation options, also the simulations are run conditionally or unconditionally.

11 Getting started

For getting a first acquaintance with the model, one may use the data set collected by Gerhard van de Bunt, discussed extensively in van de Bunt (1999), van de Bunt, van Duijn, and Snijders (1999), and used as example also in Snijders (2001) and Snijders (2005). The data files are provided with the program and at the SIENA website. The digraph data files used are the two networks vrnd32t2.dat, vrnd32t4.dat. The networks are coded as 0 = unknown, 1 = best friend, 2 = friend, 3 = friendly relation, 4 = neutral, 5 = troubled relation, 6 = item non-response, 9 = actor non-response. Choose the values 1, 2, and 3 as the values to be coded as 1 for the first as well as the second network. Choose 6 and 9 as missing data codes.

The actor attributes are in the file vars.dat. Variables are, respectively, gender (1 = F, 2 = M), program, and smoking (1 = yes, 2 = no). See the references mentioned above for further information about this network and the actor attributes.

At first, leave the specification of the rate function as it is by default (see Section 5): a constant rate function).

Then let the program estimate the parameters. You will see a screen with intermediate results: current parameter values, the differences ('deviation values') between simulated and observed statistics (these should average out to 0 if the current parameters are close to the correct estimated value), and the quasi-autocorrelations discussed in Section 6.

It is possible to intervene in the algorithm by clicking on the appropriate buttons: the algorithm may be restarted or terminated. In most cases this is not necessary.

Some patience is needed to let the machine complete its three phases. After having obtained the outcomes of the estimation process, the model can be respecified: non-significant effects may be excluded (but it is advised always to retain the out-degree and the reciprocity effects) and other effects may be included.

11.1 Model choice

For the selection of an appropriate model for a given data set it is best to start with a simple model (including, e.g., 2 or 3 effects), delete non-significant effects, and add further effects in groups of 1 to 3 effects. Like in regression analysis, it is possible that an effect that is non-significant in a given model may become significant when other effects are added or deleted!

When you start working with a new data set, it is often helpful first to investigate the main endogenous network effects (reciprocity, transitivity, etc.) to get an impression of what the network dynamics looks like, and later add effects of covariates. The most important effects are discussed in Section 5; the effects are defined mathematically in Section 13.

11.1.1 Exploring which effects to include

The present section describes an exploratory approach to model specification. A more advanced approach to testing model specifications is described in Section 8.

For an exploration of further effects to be included, the following steps may be followed:

1. Estimate a model which includes a number of basic effects;
2. Simulate the model for these parameter values but also include some other relevant statistics among the simulated statistics;
3. Look at the t-values for these other statistics; effects with large t-values are candidates for inclusion in a next model.

It should be kept in mind, however, that this exploratory approach may lead to capitalization on chance, and also that the t-value obtained as a result of the straight simulations is conditional on the fixed parameter values used, without taking into account the fact that these parameter values are estimated themselves.

It is possible that for some model specifications the data set will lead to divergence, e.g., because the data contains too little information about this effect, or because some effects are 'collinear' with each other. In such cases one must find out which are the effects causing problems, and leave these out of the model. Simulation can be helpful to distinguish between the effects which should be fixed at a high positive or negative value and the effects which should be left out because they are superfluous.

When the distribution of the out-degrees is fitted poorly an improvement usually is possible either by including non-linear effects of the out-degrees in the evaluation function.

11.2 Convergence problems

If there are convergence problems, this may have several reasons.

- The data specification was incorrect (e.g., because the coding was not given properly).
- The starting values were poor. Try restarting from the standard initial values (a certain non-zero value for the density parameter, and zero values for the other parameters); or from values obtained as the estimates for a simpler model that gave no problems. The initial default parameter values can be obtained by choosing the model option "standard initial values".
- The model does not fit well in the sense that even with well-chosen parameters it will not give a good representation of the data.

  This can be the case, e.g., when there is a large heterogeneity between the actors which is not well represented by effects of covariates. The out-degrees and in-degrees are given in the begin of the SIENA output to be able to check whether there are outlying actors having very high in- or out-degrees, or a deviating dynamics in their degrees. Strong heterogeneity between the actors will have to be represented by suitable covariates; if these are not available, one may define one or a few dummy variables each representing an outlying actor, and give this dummy variable an ego effect in the case of deviant out-degrees, and an alter effect in the case of deviant in-degrees.

  Another possibility is that there is time heterogeneity. Indications about this can be gathered also from the descriptives given in the start of the output file: the number of changes upward and downward, in the network and also – if any – in the dependent behavioral variable. If these do not show a smooth or similar pattern across the observations, then it may be useful to include actor variables representing time trends. These could be smooth – e.g., linear – but they also could be dummy variables representing one or more observational periods; these must be included as an ego effect to represent time trends in the tendency to make ties (or to display higher values of the behavior in question).
- Too many weak effects are included. Use a smaller number of effects, delete non-significant ones, and increase complexity step by step. Retain parameter estimates from the last (simpler) model as the initial values for the new estimation procedure, provided for this model the algorithm converged without difficulties.

- Two or more effects are included that are almost collinear in the sense that they can both explain the same observed structures. This will be seen in high absolute values of correlations between parameter estimates. In this case it may be better to exclude one of these effects from the model.
- An effect is included that is large but of which the precise value is not well-determined (see above: section on fixing parameters). This will be seen in estimates and standard errors both being large and often in divergence of the algorithm. Fix this parameter to some large value. (Note: large here means, e.g., more than 5 or less than -5; depending on the effect, of course.)

If the algorithm is unstable, with parameter values (the left hand list in the SIENA window) changing too wildly, or with the algorithm suddenly seeming stuck and not moving forward, the a solution may be to simplify the model (perhaps later on making it more complex again in forward parameter estimation steps); another solution may be to decrease the initial gain parameter (see Section 10).

12 Multilevel network analysis

For combining SIENA results of several independent networks, there are three options. ('Independent' networks here means that the sets of actors are disjoint, and it may be assumed that there are no direct influences from one network to another.) The first two options assume that the parameters of the actor-based models for the different networks are the same – except for the basic rate parameters and for those differences that are explicitly modeled by interactions with dummy variables indicating the different networks. The first and third options require that the number of observations is the same for the different networks. This is not required for the second option. These methods can be applied for two or more networks.

The three options are:

1. Combining the different networks in one large network, indicating by structural zeros that ties between the networks are not permitted. This is explained in Section 4.1.1.
   The special effort to be made here is the construction of the data files for the large (combined) network.

2. Combining different sub-projects into one *multi-group* project. The 'sub-projects' are the same as the 'different networks' mentioned here. This is explained in Section 12.1.
   A difference between options 1 and 2 is that the use of structural zeros (option 1) will lead to a default specification where the rate parameters are equal across networks (this can be changed by making the rate dependent upon dummy actor variables that indicate the different networks) whereas the multi-group option yields rate parameters that are distinct across different networks.

3. Analyzing the different networks separately, without any assumption that parameters are the same but using the same model specification, and post-processing the output files by a meta-analysis using Siena08. This is explained in Section 12.2.

The first and second options will yield nearly the same results, with the differences depending on the basic rate (and perhaps other) parameters that are allowed to differ between the different networks, and of course also depending on the randomness of the estimation algorithm. The second option is more 'natural' given the design of SIENA and will normally run faster than the first. Therefore the second option seems preferable to the first.

The third option makes much less assumptions because parameters are not constrained at all across the different networks. Therefore the arguments usual in statistical modeling apply: as far as assumptions is concerned, option 3 is safer; but if the assumptions are satisfied (or if they are a good approximation), then options 1 and 2 have higher power and are simpler. However, option 3 requires that each of the different network data sets is informative enough to lead to well-converged estimates; this will not always be the case for small data sets, and then options 1 or 2 are preferable.

When the data sets for the different networks are not too small individually, then a middle ground might be found in the following way. Start with option 3. This will show for which parameters there are important differences between the networks. Next follow option 2, with interactions between the sub-project dummies and those parameters for which there were important between-network differences. This procedure may work less easily when the number of different networks is relatively high, because it may then lead to too many interactions with dummy variables.

12.1 Multi-group Siena analysis

The multi-group option 'glues' several projects (further referred to as *sub-projects*) after each other into one larger multi-group project. These sub-projects must have the same sets of variables of

all kinds: that is, the list of dependent networks, dependent behavioral variables, actor covariates, and dyadic covariates must be the same for the various sub-projects. The number of actors and the number of observations can be different, however. These sub-projects then are combined into one project where the number of actors is the largest of the number of actors of the sub-projects, and the number of observations is the sum of the observations of the sub-projects. As an example, suppose that three projects with names `sub1`, `sub2`, and `sub3` are combined. Suppose `sub1` has 21 actors and 2 observations, `sub2` has 35 actors and 4 observations, and `sub3` has 24 actors with 5 observations. Then the combined multi-group project has 35 actors and 11 observations. The step from observation 2 to 3 switches from sub-project `sub1` to sub-project `sub2`, while the step from observation 6 to 7 switches from sub-project `sub2` to `sub3`. These switching steps do not correspond to simulations of the actor-based model, because that would not be meaningful.

The different sub-projects are considered to be unrelated except that they have the same model specification and the same parameter values.

Given the potentially large number of periods that can be implied by the multi-group option, it probably is advisable, when using Method of Moments estimation, to use the conditional estimation option.

In SIENA version 4 the groups can be specified directly.

12.2 Meta-analysis of Siena results

The program Siena08.exe is a relatively simple multilevel extension to SIENA. This program must be run independently, after having obtained estimates for a common model estimated for several data sets. Siena08 combines the estimates in a meta-analysis or multilevel analysis according to the methods of Snijders and Baerveldt (2003), and according to a Fisher-type combination of one-sided p-values. This combination method of Fisher (1932) is described in Hedges and Olkin (1985) and (briefly) in Snijders and Bosker (1999, Chapter 3). Some more information is at the SIENA website.

For SIENA version 4 the program Siena08.exe still must be checked and adapted. We hope that its role will be taken over by new functions in RSiena.

All SIENA output files to be used must already exist, and the *last estimation results* in these output files will be used. It is required that all these last estimation runs have the same set of estimated parameters, and of parameters tested by score tests. The program does not check that the score tests (if any) in the output files refer to the same parameters. It is also required that the decimal separator is a point, not a comma. (This depends on your Windows settings; if your output files have commas, just change all commas into points using an editor.) The Siena08 project is the collection of output files to be combined, which is defined in the project .mli file.

An easy way to operate Siena08 is to make a batch file containing the single line

```
Siena08 ABC
```

where ABC is the projectname.

E.g., suppose the projectname is ABC. Then there must be a project file with the name ABC.mli (the root name "ABC" can be chosen by the user, the extension name "mli" is prescribed.) If the number of network evolution projects combined in this Siena08 run is given by K, e.g. the $K = 3$ projects with names A, B and C, then the file ABC.mli must give the project names on separate lines and in addition the options, as indicated in the following example file:

```
[This file contains specifications for the meta-analysis of Siena projects.]
[It serves as input for the Siena08 program.]

@1 [general information about the Siena project list ]
10 [number of projects, names follow:]
```

```
A
B
C

@2 [options for estimation of projects]
5 [upper bound for standard error in meta-analysis]
1 [code 0=estimate, 1=aggregate from .out-files, 2=generate .dsc-file]
1 [code 1=extra output]
0 [number of score tests]
```

Executing the batch file (e.g. by double clicking) will execute Siena08. To get started, try this out with a small data set. Some further explanation and example data are provided on the SIENA website.

13 Mathematical definition of effects

Here, the mathematical formulae for the definition of the effects are given. In Snijders (2001, 2005) and Steglich, Snijders and Pearson, (2010), further background to these formulae can be found. The effects are grouped into effects for modelling network evolution and effects for modelling behavioral evolution (i.e., the dynamics of dependent actor variables). Within each group of effects, the effects are listed in the order in which they appear in SIENA.

For two-mode (bipartite) networks, only a subset of the effects is meaningful, since the first node set has only outgoing ties and the second only incoming; for example, the reciprocity effect is meaningless because there cannot be any reciprocal ties; the out-degree popularity effect is meaningless because it refers to incoming ties of actors with high out-degrees; and there are no similarity effects of actor covariates. There is one additional effect for two-mode networks, viz., the four-cycle effect.

Some of the effects contain a number which is denoted in this section by c, and called in this manual an *internal effect parameter*. (These are totally different from the statistical parameters which are the weights of the effects in the objective function.)

13.1 Network evolution

The model of network evolution consists of the model of actors' decisions to establish new ties or dissolve existing ties (according to *evaluation* and *endowment functions*) and the model of the timing of these decisions (according to the *rate function*). The objective function of the actor is the sum of the network evaluation function and the network endowment function

$$u^{\mathrm{net}}(x) \;=\; f^{\mathrm{net}}(x) + g^{\mathrm{net}}(x) \;, \tag{2}$$

and a random term; where the evaluation function $f^{\mathrm{net}}(x)$ and the endowment function $g^{\mathrm{net}}(x)$ are as defined in the following subsections.

For some effects the endowment function is implemented not for estimation by the Method of Moments but only by the Maximum Likelihood or Bayesian method; this is indicated below by "endowment effect only likelihood-based".

(It may be noted that the network evaluation function was called objective function, and the endowment function was called gratification function, in Snijders, 2001.)

13.1.1 Network evaluation function

The network evaluation function for actor i is defined as

$$f^{\mathrm{net}}(x) \;=\; \sum_k \beta_k^{\mathrm{net}} s_{ik}^{\mathrm{net}}(x) \tag{3}$$

where β_k^{net} are parameters and $s_{ik}^{\mathrm{net}}(x)$ are effects as defined below.

The potential effects in the network evaluation function are the following. Note that in all effects where a constants c occurs, this constant can be chosen and changed by the user; this is the internal effect parameter mentioned above. For non-directed networks, the same formulae are used, unless a different formula is given explicitly.

1. *out-degree effect* or *density effect*, defined by the out-degree
   $s_{i1}^{\mathrm{net}}(x) = x_{i+} = \sum_j x_{ij}$,
   where $x_{ij} = 1$ indicates presence of a tie from i to j while $x_{ij} = 0$ indicates absence of this tie;

2. *reciprocity effect*, defined by the number of reciprocated ties
$s_{i2}^{\text{net}}(x) = \sum_j x_{ij}\, x_{ji}$;

3. *transitive triplets effect*, defined by the number of transitive patterns in i's relations (ordered pairs of actors (j,h) to both of whom i is tied, while also j is tied to h),
for directed networks, $s_{i3}^{\text{net}}(x) = \sum_{j,h} x_{ij}\, x_{ih}\, x_{jh}$;
and for non-directed networks, $s_{i3}^{\text{net}}(x) = \sum_{j<h} x_{ij}\, x_{ih}\, x_{jh}$;
there was an error here until version 3.313, which amounted to combining the transitive triplets and transitive mediated triplets effects;

4. *transitive mediated triplets effect*, defined by the number of transitive patterns in i's relations where i has the mediating position (ordered pairs of actors (j,h) for which j is tied to i and i to h, while also j is tied to h), which is different from the transitive triplets effect only for directed networks,
$s_{i4}^{\text{net}}(x) = \sum_{j,h} x_{ji}\, x_{ih}\, x_{jh}$;
this cannot be used together with the transitive triplets effect in Method of Moments estimation, because of perfect collinearity of the fit statistics;

5. *number of 3-cycles*,
$s_{i5}^{\text{net}}(x) = \sum_{j,h} x_{ij}\, x_{jh}\, x_{hi}$;

6. for two-mode networks: the *number of 4-cycles*,
$s_{i6}^{\text{net}}(x) = \sum_{i_1,i_2,j_1,j_2} x_{i_1 j_1}\, x_{i_1 j_2}\, x_{i_2 j_1}\, x_{i_2 j_2}$;

7. *transitive ties effect* (earlier called *(direct and indirect ties) effect*), defined by the number of actors to whom i is directly as well as indirectly tied,
$s_{i7}^{\text{net}}(x) = \sum_j x_{ij}\ \max_h(x_{ih}\, x_{hj})$;

8. *betweenness count*,
$s_{i8}^{\text{net}}(x) = \sum_{j,h} x_{hi}\, x_{ij}\, (1 - x_{hj})$;

9. *balance*, defined by the similarity between the outgoing ties of actor i and the outgoing ties of the other actors j to whom i is tied,

$$s_{i9}^{\text{net}}(x) = \sum_{j=1}^{n} x_{ij} \sum_{\substack{h=1 \\ h\neq i,j}}^{n} (b_0 - \mid x_{ih} - x_{jh} \mid) \ ,$$

where b_0 is a constant included to reduce the correlation between this effect and the density effect, defined by

$$b_0 = \frac{1}{(M-1)n(n-1)(n-2)} \sum_{m=1}^{M-1} \sum_{i,j=1}^{n} \sum_{\substack{h=1 \\ h\neq i,j}}^{n} \mid x_{ih}(t_m) - x_{jh}(t_m) \mid \ .$$

(In SIENA versions before 3.324, this was divided by $n-2$, which for larger networks tended to lead to quite large estimates and standard errors. Therefore in version 3.324, the division by $n-2$ – which had not always been there – was dropped.)

10. *number of distances two effect*, defined by the number of actors to whom i is indirectly tied (through at least one intermediary, i.e., at sociometric distance 2),
$s_{i10}^{\text{net}}(x) = \#\{j \mid x_{ij} = 0,\ \max_h(x_{ih}\, x_{hj}) > 0\}$;
endowment effect only likelihood-based;

11. *number of doubly achieved distances two effect*, defined by the number of actors to whom i is not directly tied, and tied through twopaths via at least two intermediaries,
$s^{\text{net}}_{i11}(x) = \#\{j \mid x_{ij} = 0, \sum_h (x_{ih}\, x_{hj}) \geq 2\}$;
endowment effect only likelihood-based;

12. *number of dense triads*, defined as triads containing at least c ties,
$s^{\text{net}}_{i12}(x) = \sum_{j,h} x_{ij}\, I\{x_{ij} + x_{ji} + x_{ih} + x_{hi} + x_{jh} + x_{hj}) \geq c\}$,
where the 'indicator function' $I\{A\}$ is 1 if the condition A is fulfilled and 0 otherwise, and where c is either 5 or 6;
(this effect is superfluous and undefined for symmetric networks);

13. *number of (unilateral) peripheral relations to dense triads*,
$s^{\text{net}}_{i13}(x) = \sum_{j,h,k} x_{ij}(1 - x_{ji})(1 - x_{hi})(1 - x_{ki}) I\{(x_{jh} + x_{hj} + x_{jk} + x_{kj} + x_{hk} + x_{kh}) \geq c\}$,
where c is the same constant as in the *dense triads* effect;
for symmetric networks, the 'unilateral' condition is dropped, and the definition is
$s^{\text{net}}_{i13}(x) = \sum_{j,h,k} x_{ij}(1 - x_{hi})(1 - x_{ki}) I\{(x_{jh} + x_{hj} + x_{jk} + x_{kj} + x_{hk} + x_{kh}) \geq c\}$;

14. *in-degree related popularity effect* (earlier called *popularity* or *popularity of alter effect*), defined by the sum of the in-degrees of the others to whom i is tied,
$s^{\text{net}}_{i14}(x) = \sum_j x_{ij}\, x_{+j} = \sum_j x_{ij} \sum_h x_{hj}$;
until version 3.313, this effect was multiplied by a factor $1/n$;

15. *in-degree related popularity (sqrt) effect* (earlier called *popularity of alter (sqrt measure) effect*), defined by the sum of the square roots of the in-degrees of the others to whom i is tied,
$s^{\text{net}}_{i15}(x) = \sum_j x_{ij} \sqrt{x_{+j}} = \sum_j x_{ij} \sqrt{\sum_h x_{hj}}$;
this often works better in practice than the raw popularity effect; also it is often reasonable to assume that differences between high in-degrees are relatively less important than the same differences between low in-degrees;

16. *out-degree related popularity effect* (earlier called *activity* or *activity of alter effect*), defined by the sum of the out-degrees of the others to whom i is tied,
$s^{\text{net}}_{i16}(x) = \sum_j x_{ij}\, x_{j+} = \sum_j x_{ij} \sum_h x_{jh}$;
until version 3.313, this effect was multiplied by a factor $1/n$;

17. *out-degree related popularity (sqrt) effect* (earlier called *activity of alter (sqrt measure) effect*), defined by the sum of the square roots of the out-degrees of the others to whom i is tied,
$s^{\text{net}}_{i17}(x) = \sum_j x_{ij} \sqrt{x_{j+}} = \sum_j x_{ij} \sqrt{\sum_h x_{jh}}$;
this often works better in practice than the raw activity effect for the same reasons as mentioned above for the sqrt measure of the popularity effect;

⊙ for non-directed networks, the popularity and activity effects are taken together as "degree effects", since in-degrees and out-degrees are the same in this case;

18. *in-degree related activity effect*, defined as the cross-product of the actor's in- and out-degrees,
$s^{\text{net}}_{i18}(x) = x_{i+}\, x_{+i}$;
endowment effect only likelihood-based;

19. *in-degree related activity (sqrt) effect*, defined by
$s^{\text{net}}_{i19}(x) = x_{i+} \sqrt{x_{+i}}$;

20. *out-degree related activity effect*, defined as the squared out-degree of the actor, $s^{\text{net}}_{i20}(x) = x^2_{i+}$;
endowment effect only likelihood-based;

21. *out-degree related activity (sqrt) effect* (earlier called *out-degree^(1.5)*), defined by
$s_{i21}^{\text{net}}(x) = x_{i+}^{1.5} = x_{i+}\sqrt{x_{i+}}$
endowment effect only likelihood-based;

22. *out-degree up to c*, where c is some constant (internal effect parameter, see above), defined by
$s_{i22}^{\text{net}}(x) = \max(x_{i+}, c)$;
this is left out in later versions of SIENA;

23. *square root out-degree*, defined by
$s_{i23}^{\text{net}}(x) = \sqrt{x_{i+}}$;
this is left out in later versions of SIENA;

24. *squared (out-degree – c)*, where c is some constant, defined by
$s_{i24}^{\text{net}}(x) = (x_{i+} - c)^2$,
where c is chosen to diminish the collinearity between this and the density effect;
this is left out in later versions of SIENA;

25. *sum of (1/(out-degree + c)*, where c is some constant, defined by
$s_{i25}^{\text{net}}(x) = 1/(x_{i+} + c)$;
endowment effect only likelihood-based;

26. *sum of (1/(out-degree + c)(out-degree + c + 1))*, where c is some constant, defined by
$s_{i26}^{\text{net}}(x) = 1/(x_{i+} + c)(x_{i+} + c + 1)$;
endowment effect only likelihood-based.

27. *out-out degree^(1/c) assortativity*, which represents the differential tendency for actors with high out-degrees to be tied to other actors who likewise have high out-degrees,
$s_{i27}^{\text{net}}(x) = \sum_j x_{ij}\, x_{i+}^{1/c} x_{j+}^{1/c}$;
c can be 1 or 2 (the latter value is the default);

28. *out-in degree^(1/c) assortativity*, which represents the differential tendency for actors with high out-degrees to be tied to other actors who have high in-degrees,
$s_{i28}^{\text{net}}(x) = \sum_j x_{ij}\, x_{i+}^{1/c} x_{+j}^{1/c}$;
c can be 1 or 2 (the latter value is the default);

29. *in-out degree^(1/c) assortativity*, which represents the differential tendency for actors with high in-degrees to be tied to other actors who have high out-degrees,
$s_{i29}^{\text{net}}(x) = \sum_j x_{ij}\, x_{+i}^{1/c} x_{j+}^{1/c}$;
c can be 1 or 2 (the latter value is the default);

30. *in-in degree^(1/c) assortativity*, which represents the differential tendency for actors with high in-degrees to be tied to other actors who likewise have high in-degrees,
$s_{i30}^{\text{net}}(x) = \sum_j x_{ij}\, x_{+i}^{1/c} x_{+j}^{1/c}$;
c can be 1 or 2 (the latter value is the default);

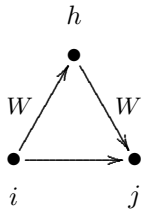
The effects for a dyadic covariate w_{ij} are

31. *covariate (centered) main effect*,
$s_{i31}^{\text{net}}(x) = \sum_j x_{ij}\,(w_{ij} - \bar{w})$
where $\bar{w}$ is the mean value of w_{ij} ;

32. *covariate (centered) × reciprocity*,
$s_{i32}^{\text{net}}(x) = \sum_j x_{ij} x_{ji}\,(w_{ij} - \bar{w})$.

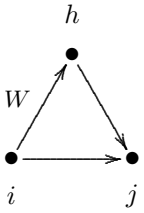
⊙ Three different ways can be modeled in which a triadic combination can be made between the dyadic covariate and the network. In the explanation, the dyadic covariate is regarded as a weighted network (which will be reduced to a non-weighted network if w_{ij} only assumes the values 0 and 1). By way of exception, the dyadic covariate is not centered in these three effects (to make it better interpretable as a network). In the text and the pictures, an arrow with the letter W represents a tie according to the weighted network W.

33. *WW => X closure of covariate*,
$s^{\text{net}}_{i33}(x) = \sum_{j \neq h} x_{ij}\, w_{ih}\, w_{hj}$;
this refers to the closure of $W - W$ two-paths; each $W - W$ two-path $i \overset{W}{\rightarrow} h \overset{W}{\rightarrow} j$ is weighted by the product $w_{ih}w_{hj}$ and the sum of these product weights measures the strength of the tendency toward closure of these $W - W$ twopaths by a tie.

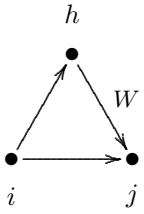


Since the dyadic covariates are represented by square arrays and not by edgelists, this will be a relatively time-consuming effect if the number of nodes is large.

34. *WX => X closure of covariate*,
$s^{\text{net}}_{i34}(x) = \sum_{j \neq h} x_{ij}\, w_{ih}\, x_{hj}$;
this refers to the closure of mixed $W - X$ two-paths; each $W - X$ two-path $i \overset{W}{\rightarrow} h \rightarrow j$ is weighted by w_{ih} and the sum of these weights measures the strength of the tendency toward closure of these mixed $W - X$ twopaths by a tie;



35. *XW => X closure of covariate*,
$s^{\text{net}}_{i35}(x) = \sum_{j \neq h} x_{ij}\, x_{ih}\, w_{hj}$;
this refers to the closure of mixed $X - W$ two-paths; each $X - W$ two-path $i \rightarrow h \overset{W}{\rightarrow} j$ is weighted by w_{hj} and the sum of these weights measures the strength of the tendency toward closure of these mixed $X - W$ twopaths by a tie.



For actor-dependent covariates v_j (recall that these are centered internally by SIENA) as well as for dependent behavior variables (for notational simplicity here also denoted v_j; these variables also are centered), the following effects are available:

36. *covariate-alter* or *covariate-related popularity*, defined by the sum of the covariate over all actors to whom i has a tie,
$s^{\text{net}}_{i36}(x) = \sum_j x_{ij}\, v_j$;

37. *covariate squared - alter* or *squared covariate-related popularity*, defined by the sum of the squared centered covariate over all actors to whom i has a tie, (not included if the variable has range less than 2)
$s^{\text{net}}_{i37}(x) = \sum_j x_{ij}\, v_j$;

38. *covariate-ego* or *covariate-related activity*, defined by i's out-degree weighted by his covariate value,
$s^{\text{net}}_{i38}(x) = v_i\, x_{i+}$;

39. *covariate-related similarity*, defined by the sum of centered similarity scores sim_{ij}^{v} between i and the other actors j to whom he is tied,
$s_{i39}^{\mathrm{net}}(x) = \sum_j x_{ij}(\mathrm{sim}_{ij}^{v} - \widehat{\mathrm{sim}^{v}})$,
where $\widehat{\mathrm{sim}^{v}}$ is the mean of all similarity scores, which are defined as $\mathrm{sim}_{ij}^{v} = \frac{\Delta - |v_i - v_j|}{\Delta}$ with $\Delta = \max_{ij} |v_i - v_j|$ being the observed range of the covariate v (this mean is given in the output file just before the "initial data description");

40. *covariate-related similarity* × *reciprocity*, defined by the sum of centered similarity scores for all reciprocal dyads in which i is situated,
$s_{i40}^{\mathrm{net}}(x) = \sum_j x_{ij}x_{ji}(\mathrm{sim}_{ij}^{v} - \widehat{\mathrm{sim}^{v}})$;

41. *same covariate*, which can also be called *covariate-related identity*, defined by the number of ties of i to all other actors j who have exactly the same value on the covariate,
$s_{i41}^{\mathrm{net}}(x) = \sum_j x_{ij}\, I\{v_i = v_j\}$,
where the indicator function $I\{v_i = v_j\}$ is 1 if the condition $\{v_i = v_j\}$ is satisfied, and 0 if it is not;

42. *same covariate* × *reciprocity*, defined by the number of reciprocated ties between i and all other actors j who have exactly the same value on the covariate,
$s_{i42}^{\mathrm{net}}(x) = \sum_j x_{ij}x_{ji}\, I\{v_i = v_j\}$;

43. *covariate-ego* × *alter*, defined by the product of i's covariate and the sum of those of his alters,
$s_{i43}^{\mathrm{net}}(x) = v_i \sum_j x_{ij}\, v_j$;

44. *covariate-ego* × *alter* × *reciprocity*, defined by the product of i's covariate and the sum of those of his reciprocated alters,
$s_{i44}^{\mathrm{net}}(x) = v_i \sum_j x_{ij}\, x_{ji}\, v_j$;

45. *ego* > *alter for covariate*, defined by the number of ties where i's covariate is larger than alter's, while equality counts for half,
$s_{i45}^{\mathrm{net}}(x) = \sum_j x_{ij}\, \mathrm{dsign}(v_i - v_j)$,
where $\mathrm{dsign}(d) = 0$ for $d < 0$, 0.5 for $d = 0$, and 1 for $d > 0$.

46. *covariate of indirect ties*, defined by the sum of the covariate over the actors to whom i is tied indirectly (at a geodesic distance of 2),
$s_{i46}^{\mathrm{net}}(x) = \sum_j (1 - x_{ij})\big(\max_h x_{ih}x_{hj}\big)v_j$.

13.1.2 Multiple network effects

If there are multiple dependent networks, the definition of cross-network effects is such that always, one network has the role of the dependent variable, while the other network, or networks, have the role of explanatory variable(s). In the following list the network in the role of dependent variable is denoted by the tie variables x_{ij}, while the tie variables w_{ij} denote the network that is the explanatory variable.

In the SIENA output for projects with multiple networks, the dependent network in each given effect is indicated by the first part of the effect name. In the list below, a more or less normally formulated name is given first, then the name used in SIENA between parentheses, using X as the name for the dependent network and W as the name for the explanatory network. Since this is a co-evolution model, SIENA will include also the effects where the roles of X and W are reversed.

The first three effects are dyadic. The first can be regarded as a main effect; the reciprocity and mutuality effects will require rather big data sets to be empirically distinguished from each other.

1. *Effect of W on X* (X: W),
   $s^{\text{net}}_{i1}(x) = \sum_j x_{ij}\, w_{ij}$;
   $i \overset{W}{\rightarrow} j$ leads to $i \overset{X}{\rightarrow} j$;

2. *Effect of incoming W on X* (X: reciprocity with W),
   $s^{\text{net}}_{i2}(x) = \sum_j x_{ij}\, w_{ji}$;
   this can be regarded as generalized exchange: $j \overset{W}{\rightarrow} i$ leads to $i \overset{X}{\rightarrow} j$;

3. *Effect of mutual ties in W on X* (X: mutuality with W),
   $s^{\text{net}}_{i3}(x) = \sum_j x_{ij}\, w_{ij}\, w_{ji}$;
   $j \overset{W}{\leftrightarrow} i$ leads to $i \overset{X}{\rightarrow} j$;

The following five are degree-related effects, where nodal degrees in the W network have effects on popularity or activity in the X network. They use an internal effect parameter p, which mostly will be 1 or 2.

To decrease correlation with other effects, the W-degrees are centered by subtracting the value $\bar{w}$, which is the average degree of W across all observations.
THIS VALUE SHOULD BE GIVEN AS THE AVERAGE DEGREE IN THE INITIAL PART OF THE OUTPUT.

4. *Effect of in-degree in W on X-popularity* (X: indegree$^{1/p}$ W popularity) defined by the sum of the W-in-degrees of the others to whom i is tied, for parameter $p = 2$ the square roots of the W-in-degrees:
   $s^{\text{net}}_{i4}(x) = \sum_j x_{ij}\, (w_{+j} - \bar{w})^{1/p}$;

5. *Effect of in-degree in W on X-activity* (X: indegree$^{1/p}$ W activity) defined by the W-in-degrees of i (for $p = 2$ its square root) times i's X-out-degree:
   $s^{\text{net}}_{i5}(x) = \sum_j x_{ij}\, (w_{+i} - \bar{w})^{1/p} = x_{i+}\, (w_{+i} - \bar{w}_{+.})^{1/p}$;

6. *Effect of out-degree in W on X-popularity* (X: outdegree$^{1/p}$ W popularity) defined by the sum of the W-out-degrees of the others to whom i is tied, for parameter $p = 2$ the square roots of the W-out-degrees:
   $s^{\text{net}}_{i6}(x) = \sum_j x_{ij}\, (w_{j+} - \bar{w})^{1/p}$;

7. *Effect of out-degree in W on X-activity* (X: outdegree$^{1/p}$ W activity) defined by the W-out-degrees of i (for $p = 2$ its square root) times i's X-out-degree:
   $s^{\text{net}}_{i7}(x) = \sum_j x_{ij}\, (w_{i+} - \bar{w})^{1/p} = x_{i+}\, (w_{i+} - \bar{w})^{1/p}$;

8. *Effect of both in-degrees in W on X-popularity* (X: both indegrees$^{1/p}$ W) defined by the sum of the W-in-degrees of the others to whom i is tied multiplied by the centered W-in-degree of i, for parameter $p = 2$ the square roots of the W-in-degrees:
   $s^{\text{net}}_{i8}(x) = \sum_j x_{ij}\, (w_{+i} - \bar{w})^{1/p}\, (w_{+j} - \bar{w})^{1/p}$;
   this can be regarded as an interaction between the effect of W-in-degree on X-popularity and the effect of W-in-degree on X-activity.

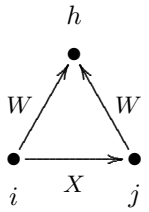
The betweenness effect is another positional effect: a positional characteristic in the W network affects the ties in the X network, but now the position is the betweenness count, defined as the

number of pairs of nodes that are not directly connected: $j \overset{W}{\nrightarrow} h$, but that are connected through i: $j \overset{W}{\rightarrow} i \overset{X}{\rightarrow} h$. Again there is an internal effect parameter p, usually 1 or 2.

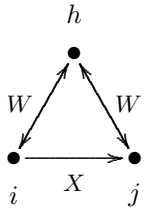
9. *Effect of W-betweenness on X-popularity* (X: betweenness$^{1/p}$ W popularity) defined by the sum of the W-betweenness counts of the others to whom i is tied:
$s_{i9}^{\text{net}}(x) = \sum_j x_{ij} \left(\sum_{h,k;h\neq k} w_{hj}\, w_{jk}\, (1 - w_{hk}) \right)^{1/p}$;

Finally there are four mixed triadic effects.

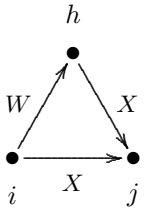
10. *agreement about W leading to X*, (X: from W agreement)
$s_{i10}^{\text{net}}(x) = \sum_{j\neq h} x_{ij}\, w_{ih}\, w_{jh}$;
this refers to agreement of actors with respect to their W-choices (structural equivalence with respect to outgoing W-choices) the contribution of the tie $i \overset{X}{\rightarrow} j$ is proportional to the number of joint W choices of others, $i \overset{W}{\rightarrow} h \overset{W}{\leftarrow} j$.



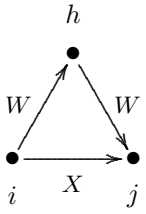
11. *agreement in mutual W-ties leading to X*, (X: from W mutual agreement)
$s_{i11}^{\text{net}}(x) = \sum_{j\neq h} x_{ij}\, w_{ih}\, w_{hi}\, w_{jh}\, w_{hj}$;
this refers to agreement of actors with respect to their mutual W-choices (structural equivalence with respect to mutual W-choices) the contribution of the tie $i \overset{X}{\rightarrow} j$ is proportional to the number of joint mutual W choices of others, $i \overset{W}{\leftrightarrow} h \overset{W}{\leftrightarrow} j$.



12. *W leading to agreement in X*, (X: W to agreement)
$s_{i12}^{\text{net}}(x) = \sum_{j\neq h} x_{ij}\, w_{ih}\, x_{hj}$;
this refers to the closure of mixed $W - X$ two-paths; the contribution of the tie $i \overset{X}{\rightarrow} j$ is proportional to the number of mixed $W - x$ two-paths $i \overset{W}{\rightarrow} h \overset{X}{\rightarrow} j$.
Note that since this is the evaluation function for actor i with respect to network X, only the x_{ij} tie indicator in the formula, corresponding to the tie $i \overset{X}{\rightarrow} j$, is the dependent variable here.
The interpretation is that actors have the tendency to make the same outgoing X-choices as those to whom they have a W-tie.



13. *mixed WW => X closure*, (X: closure of W)
$s_{i13}^{\text{net}}(x) = \sum_{j\neq h} x_{ij}\, w_{ih}\, w_{hj}$;
this refers to the closure of $W - W$ two-paths; the contribution of the tie $i \overset{X}{\rightarrow} j$ is proportional to the number of $W - W$ two-paths $i \overset{W}{\rightarrow} h \overset{W}{\rightarrow} j$.
The interpretation is that actors have the tendency to make and maintain X-ties to those to whom they have an indirect (distance 2) W-tie: 'W-ties of W-ties tend to become X-ties'.



13.1.3 Network endowment function

The network endowment function is the way of modeling effects which operate in different strengths for the creation and the dissolution of relations. The network endowment function is zero for creation of ties, and is given by

$$g^{\text{net}}(x) = \sum_k \gamma_k s_{ik}^{\text{net}}(x) \tag{4}$$

for dissolution of ties. In this formula, the γ_k are the parameters for the endowment function. The potential effects $s_{ik}^{\text{net}}(x)$ in this function, and their formulae, are the same as in the evaluation function; except that not all are available, as indicated in the preceding subsection. For further explication, consult Snijders (2001, 2005; here, the 'gratification function' is used rather than the endowment function), Snijders, Steglich, and Schweinberger (2007), and Steglich, Snijders and Pearson (2010).

13.1.4 Network rate function

The network rate function λ^{net} (lambda) is defined for Model Type 1 (which is the default Model Type) as a product

$$\lambda_i^{\text{net}}(\rho, \alpha, x, m) = \lambda_{i1}^{\text{net}} \lambda_{i2}^{\text{net}} \lambda_{i3}^{\text{net}}$$

of factors depending, respectively, on period m, actor covariates, and actor position (see Snijders, 2001, p. 383). The corresponding factors in the rate function are the following:

1. The dependence on the period can be represented by a simple factor

   $$\lambda_{i1}^{\text{net}} = \rho_m^{\text{net}}$$

   for $m = 1, ..., M-1$. If there are only $M = 2$ observations, the basic rate parameter is called ρ^{net}.

2. The effect of actor covariates with values v_{hi} can be represented by the factor

   $$\lambda_{i2}^{\text{net}} = \exp(\sum_h \alpha_h \, v_{hi}) \, .$$

3. The dependence on the position of the actor can be modeled as a function of the actor's out-degree, in-degree, and number of reciprocated relations, the 'reciprocated degrees'. Define these by

   $$x_{i+} = \sum_j x_{ij}, \;\; x_{+i} = \sum_j x_{ji}, \;\; x_{i(r)} = \sum_j x_{ij} x_{ji}$$

   (recalling that $x_{ii} = 0$ for all i).

   The contribution of the out-degrees to $\lambda_{i3}^{\text{net}}$ is a factor

   $$\exp(\alpha_h \, x_{i+}) \, ,$$

   if the associated parameter is denoted α_h for some h, and similarly for the contributions of the in-degrees and the reciprocated degrees.

Also an exponential dependence on reciprocals of out-degrees can be specified; this can be meaningful because the rate effect of the out-degree becoming a value 1 higher might become smaller and smaller as the out-degree increases. Denoting again the corresponding parameter by α_h (but always for different index numbers h), this effect multiplies the factor $\lambda_{i3}^{\text{net}}$ by

$$\exp(\alpha_h / x_{i+}) \ .$$

13.2 Behavioral evolution

The model of the dynamics of a dependent actor variable consists of a model of actors' decisions (according to *evaluation* and *endowment functions*) and a model of the timing of these decisions (according to a *rate function*), just like the model for the network dynamics. The decisions now do not concern the creation or dissolution of network ties, but whether an actor increases or decreases his score on the dependent actor variable by one, or keeps it as it is.

13.2.1 Behavioral evaluation function

Effects for the behavioral evaluation function u^{beh} can be selected from the following. Here the dependent variable is transformed to have an overall average value of 0; in other words, z denotes the original input variable minus the overall mean, which is given in the output file under the heading *Reading dependent actor variables.*

1. *behavioral shape effect*,
   $s_{i1}^{\text{beh}}(x) = z_i \ ,$
   where z_i denotes the value of the dependent behavior variable of actor i;

2. *quadratic shape effect, or effect of the behavior upon itself*, where the attractiveness of further steps up the behavior 'ladder' depends on where the actor is on the ladder:
   $s_{i2}^{\text{beh}}(x) = z_i^2$.
   The position of this effect in the sequence of effects is different between versions 3 and 4 of SIENA.

3. *average similarity effect*, defined by the average of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is tied,
   $s_{i3}^{\text{beh}}(x) = x_{i+}^{-1} \sum_j x_{ij}(\text{sim}_{ij}^z - \widehat{\text{sim}^z})$;
   (and 0 if $x_{i+} = 0$) ;

4. *total similarity effect*, defined by the sum of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is tied,
   $s_{i4}^{\text{beh}}(x) = \sum_j x_{ij}(\text{sim}_{ij}^z - \widehat{\text{sim}^z})$;

5. *indegree effect*,
   $s_{i5}^{\text{beh}}(x) = z_i \sum_j x_{ji}$;

6. *outdegree effect*,
   $s_{i6}^{\text{beh}}(x) = z_i \sum_j x_{ij}$;

7. *isolate effect*, the differential attractiveness of the behavior for isolates,
   $s_{i7}^{\text{beh}}(x) = z_i I\{x_{+i} = 0\}$,
   where again $I\{A\}$ denotes the indicator function of the condition A;

8. *average similarity* × *reciprocity effect*, defined by the sum of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is reciprocally tied,
$s_{i8}^{\mathrm{beh}}(x) = x_{i(r)}^{-1} \sum_j x_{ij}x_{ji}(\mathrm{sim}_{ij}^z - \widehat{\mathrm{sim}^z})$;
(and 0 if $x_{i(r)} = 0$) ;

9. *total similarity* × *reciprocity effect*, defined by the sum of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is reciprocally tied,
$s_{i9}^{\mathrm{beh}}(x) = \sum_j x_{ij}x_{ji}(\mathrm{sim}_{ij}^z - \widehat{\mathrm{sim}^z})$;

10. *average similarity* × *popularity alter effect*, defined by the sum of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is tied, multiplied by their indegrees,
$s_{i10}^{\mathrm{beh}}(x) = x_{i+}^{-1} \sum_j x_{ij}x_{+j}(\mathrm{sim}_{ij}^z - \widehat{\mathrm{sim}^z})$;
(and 0 if $x_{i+} = 0$) ;

11. *total similarity* × *popularity alter effect*, defined by the sum of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is tied, multiplied by their indegrees,
$s_{i11}^{\mathrm{beh}}(x) = \sum_j x_{ij}x_{+j}(\mathrm{sim}_{ij}^z - \widehat{\mathrm{sim}^z})$;

12. *average similarity* × *reciprocity* × *popularity alter effect*, defined by the sum of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is reciprocally tied, multiplied by their indegrees,
$s_{i12}^{\mathrm{beh}}(x) = x_{i(r)}^{-1} \sum_j x_{ij}x_{ji}x_{+j}(\mathrm{sim}_{ij}^z - \widehat{\mathrm{sim}^z})$;
(and 0 if $x_{i(r)} = 0$) ;

13. *total similarity* × *reciprocity* × *popularity alter effect*, defined by the sum of centered similarity scores sim_{ij}^z between i and the other actors j to whom he is reciprocally tied, multiplied by their indegrees,
$s_{i13}^{\mathrm{beh}}(x) = \sum_j x_{ij}x_{ji}x_{+j}(\mathrm{sim}_{ij}^z - \widehat{\mathrm{sim}^z})$;

14. *average alter effect*, defined by the product of i's behavior multiplied by the average behavior of his alters (a kind of ego-alter behavior covariance),
$s_{i14}^{\mathrm{beh}}(x) = z_i\big(\sum_j x_{ij}\, z_j\big)/\big(\sum_j x_{ij}\big)$
(and the mean behavior, i.e. 0, if the ratio is 0/0) ;

15. *average reciprocated alter effect*, defined by the product of i's behavior multiplied by the average behavior of his reciprocated alters,
$s_{i15}^{\mathrm{beh}}(x) = z_i\big(\sum_j x_{ij}\, x_{ji}\, z_j\big)/\big(\sum_j x_{ij}\, x_{ji}\big)$
(and 0 if the ratio is 0/0) ;

16. *dense triads effect*, defined by the number of dense triads in which actor i is located,
$s_{i16}^{\mathrm{beh}}(x) = z_i \sum_{j,h} I\{x_{ij} + x_{ji} + x_{ih} + x_{hi} + x_{jh} + x_{hj}\,) \geq c\}$,
where c is either 5 or 6;
this is currently not correctly implemented in SIENA *3* ;

17. *peripheral effect*, defined by the number of dense triads to which actor i stands in a unilateral-peripheral relation,
$s_{i17}^{\mathrm{beh}}(x) = z_i \sum_{j,h,k} x_{ij}(1-x_{ji})(1-x_{hi})(1-x_{ki})I\{x_{ij} + x_{ji} + x_{ih} + x_{hi} + x_{jh} + x_{hj}\,) \geq c\}$,
where c is the same constant as in the *dense triads* effect;
for directed networks, the unilateral condition is dropped, and the effect is
$s_{i17}^{\mathrm{beh}}(x) = z_i \sum_{j,h,k} x_{ij}(1-x_{hi})(1-x_{ki})I\{x_{ij} + x_{ji} + x_{ih} + x_{hi} + x_{jh} + x_{hj}\,) \geq c\}$;
this is currently not correctly implemented in SIENA *3* ;

18. *reciprocated degree effect*,
$s^{\text{beh}}_{i18}(x) = z_i \sum_j x_{ij}\, x_{ji}$;

19. *average similarity* $\times$ *popularity ego effect*, defined by the sum of centered similarity scores sim^z_{ij} between i and the other actors j to whom he is tied, multiplied by ego's indegree,
$s^{\text{beh}}_{i19}(x) = x_{+i}\, x_{i+}^{-1} \sum_j x_{ij}(\text{sim}^z_{ij} - \widehat{\text{sim}^z})$;
(and 0 if $x_{i+} = 0$) ;
because of collinearity, under the Method of Moments this cannot be estimated together with the average similarity $\times$ popularity alter effect.

For each actor-dependent covariate v_j (recall that these are centered internally by SIENA) as well as for each of the other dependent behavior variables (for notational simplicity here also denoted v_j), there is one main effect.

13.2.2 Behavioral endowment function

Also the behavioral model knows the distinction between evaluation and endowment effects. The formulae of the effects that can be included in the behavioral endowment function e^{beh} are the same as those given for the behavioral evaluation function. However, they enter calculation of the endowment function only when the actor considers decreasing his behavioral score by one unit (downward steps), not when upward steps (or no change) are considered. For more details, consult Snijders, Steglich, and Schweinberger (2007) and Steglich, Snijders and Pearson (2010).

The statistics reported as *dec. beh.* (decrease in behavior) are the sums of the changes in actor-dependent values for only those actors who decreased in behavior. More precisely, it is

$$\sum_{m=1}^{M-1} \sum_{i=1}^{n} I\{z_i(t_{m+1}) < z_i(t_m)\} \left(s^{\text{beh}}_{ik}(x(t_{m+1})) - s^{\text{beh}}_{ik}(x(t_m))\right), \tag{5}$$

where M is the number of observations, $x(t_m)$ is the observed situation at observation m, and the indicator function $I\{A\}$ is 0 if event A is true and 0 if it is untrue.

13.2.3 Behavioral rate function

The behavioral rate function λ^{beh} consists of a constant term per period,

$$\lambda^{\text{beh}}_i = \rho^{\text{beh}}_m$$

for $m = 1, ..., M-1$.

14 Parameter interpretation

This section still is in development.

14.1 Longitudinal models

The main 'driving force' of the actor-oriented model is the evaluation function (in earlier publications called objective function, see Snijders, 2001, 2005) given in formula (3) (for the network) as

$$f^{\text{net}}(x) = \sum_k \beta_k^{\text{net}} s_{ik}^{\text{net}}(x) \ .$$

The objective function can be regarded as the "attractiveness" of the network (or behavior, respectively) for a given actor. For getting a feeling of what are small and large values, is is helpful to note that the objective functions are used to compare how attractive various different tie changes are, and for this purpose random disturbances are added to the values of the objective function with standard deviations equal[8] to 1.28.

An alternative interpretation is that when actor i is making a 'ministep', i.e., a single change in his outgoing ties (where no change also is an option), and x_a and x_b are two possible results of this ministep, then $f^{\text{net}}(x_b) - f^{\text{net}}(x_a)$ is the log odds ratio for choosing between these two alternatives – so that the ratio of the probability of x_b and x_a as next states is

$$\exp(f^{\text{net}}(x_b) - f^{\text{net}}(x_a)) \ .$$

Note that, when the current state is x, the possibilities for x_a and x_b are x itself (no change), or x with one extra outgoing tie from i, or x with one fewer outgoing tie from i. Explanations about log odds ratios can be found in texts about logistic regression and loglinear models.

The evaluation function is a weighted sum of 'effects' $s_{ik}^{\text{net}}(x)$. Their formulae can be found in Section 13.1.1. These formulae, however, are defined as a function of the whole network x, and in most cases the contribution of a single tie variable x_{ij} is just a simple component of this formula. The contribution to $s_{ik}^{\text{net}}(x)$ of adding the tie $i \to h$ minus the contribution of adding the tie $i \to j$ is the log odds ratio comparing the probabilities of i sending a new tie to h versus sending the tie to j, if all other effects $s_{ik}^{\text{net}}(x)$ yields the same values for these two hypothetical new configurations.

For example, suppose that actors j and h, actual or potential relation partners of actor i, have exactly the same network position and the same values on all variables included in the model, except that for some actor variable V for which only the popularity (alter) effect is included in the model, actor h is one unit higher than actor j: $v_h = v_j + 1$. It can be seen in Section 13.1.1 that the popularity (alter) effect is defined as

$$s_{ik}^{\text{net}}(x) = \sum_j x_{ij} \, v_j \ .$$

The contribution to this formula made by a single tie variable, i.e., the difference made by filling in $x_{ij} = 1$ or $x_{ij} = 0$ in this formula, is just v_j. Let us denote the weight of the V-alter effect by β_k. Then, the difference between extending a tie to h or to j that follows from the V-alter effect is $\beta_k \times (v_h - v_j) = \beta_k \times 1 = \beta_k$.

Thus, in this situation, β_k is the log odds ratio of the probability that h is chosen compared to the probability that j is chosen. E.g., if i currently has a tie neither to j nor to h, and supposing that $\beta_k = 0.3$, the probability for i to extend a new tie to h is $e^{0.3} = 1.35$ times as high as the probability for i to extend a new tie to j.

[8] More exactly, the value is $\sqrt{\pi^2/6}$, the standard deviation of the Gumbel distribution; see Snijders (2001).

14.1.1 Ego – alter selection tables

When some variable V occurs in several effects in the model, then its effects can best be understood by considering all these effects simultaneously. For example, if in a network dynamics model the ego, alter, and similarity effects of a variable V are specified, then the formulae for their contribution can be obtained from the components listed in Section 13.1.1 as

$$\beta_{\text{ego}}\, v_i\, x_{i+} \;+\; \beta_{\text{alter}} \sum_j x_{ij}\, v_j \;+\; \beta_{\text{sim}} \sum_j x_{ij} (\text{sim}_{ij}^v - \widehat{\text{sim}^v}) \;, \tag{6}$$

where the similarity score is $\text{sim}_{ij}^v = 1 - \frac{|v_i - v_j|}{\Delta_V}$, with $\Delta_V = \max_{ij} |v_i - v_j|$ being the observed range of the covariate v and where $\widehat{\text{sim}^v}$ is the mean of all similarity scores. The superscript $^{\text{net}}$ is left out of the notation for the parameters in order not to clutter the notation.

Similarly to how it was done above, the contribution to (6) of the tie from i to j, represented by the single tie variable x_{ij} – i.e., the difference between the values of (6) for $x_{ij} = 1$ and $x_{ij} = 0$ – can be calculated from this formula. It should be noted that all variables are internally centered by SIENA, and that the mean values used for the centering are given near the beginning of the input file. This is made explicit in the following by the subtraction of the mean $\bar{v}$. The contribution of

$$\begin{aligned} &\beta_{\text{ego}}\, (v_i - \bar{v}) \;+\; \beta_{\text{alter}}\, (v_j - \bar{v}) \;+\; \beta_{\text{sim}}\, (\text{sim}_{ij}^v - \widehat{\text{sim}^v}) \\ &= \beta_{\text{ego}}\, (v_i - \bar{v}) \;+\; \beta_{\text{alter}}\, (v_j - \bar{v}) \;+\; \beta_{\text{sim}} \left(1 - \frac{|v_i - v_j|}{\Delta_V} - \widehat{\text{sim}^v}\right) . \end{aligned} \tag{7}$$

From this equation a table can be made that gives the outcome of (7) for some values of v_i and v_j.

This can be concretely carried using the data set s50 which is an excerpt of 50 girls in the data set used in Pearson and Michell (2000), Pearson and West (2003), Steglich et al. (2006) and Steglich et al. (2007). We refer to any of these papers for a further description of the data. The friendship network data over 3 waves are in the files s50-network1.dat, s50-network2.dat, and s50-network3.dat. We also use the attribute data for alcohol use, s50-alcohol.dat, as a dependent variable. It can be seen from the SIENA output file using these data that the alcohol use variable assumes values from 1 to 5, with overall mean equal to $\bar{v} = 3.113$, and mean of the similarity variable $\widehat{\text{sim}^v} = 0.6983$. Drug use is used as a changing actor variable, with range 1–4, average $\bar{v} = 1.5$ and average dyadic similarity $\widehat{\text{sim}^v} = 0.7533$.

Suppose that we fit a model of network-behavior co-evolution to this data set with for the network evolution the effects of outdegree, reciprocity, transitive ties, number of distances two, the ego, alter, and similarity effects of alcohol use, as well as the ego, alter, and similarity effects of drug use; and for the behavior (i.e., alcohol) dynamics the shape effect, the effect of alcohol on itself (quadratic shape effect), and the average similarity effect.

The results obtained are given in the following part of the output file.

```
Network Dynamics
 1. rate:  constant network rate (period 1)          8.2357  (   1.6225)
 2. rate:  constant network rate (period 2)          5.6885  (   0.8434)
 3. eval:  outdegree (density)                      -2.1287  (   0.1565)
 4. eval:  reciprocity                               2.3205  (   0.2132)
 5. eval:  transitive ties                           0.2656  (   0.2025)
 6. eval:  number of actors at distance 2           -0.9947  (   0.2173)
 7. eval:  drink alter                               0.0899  (   0.1184)
 8. eval:  drink ego                                -0.0100  (   0.1087)
 9. eval:  drink similarity                          0.8994  (   0.5864)
10. eval:  drug use alter                           -0.1295  (   0.1282)
```

```
11. eval:  drug use ego                                  0.1362  (   0.1253)
12. eval:  drug use similarity                           0.6650  (   0.3381)

Behavior Dynamics
13. rate:  rate drink period 1                           1.3376  (   0.3708)
14. rate:  rate drink period 2                           1.8323  (   0.4546)
15. eval:  behavior drink shape                          0.3618  (   0.1946)
16. eval:  behavior drink average similarity             3.9689  (   2.2053)
17. eval:  behavior drink: effect from drink            -0.0600  (   0.1181)
```

We interpret here the parameter estimates for the effects of drinking behavior and drug use without being concerned with the significance, or lack thereof. For the drinking behavior, formula (7) yields (rounded to two decimals)

$$-0.01\,(v_i - \bar{v}) \;+\; 0.09\,(v_j - \bar{v}) \;+\; 0.90\Big(1 \;-\; \frac{|v_i - v_j|}{\Delta_V} - 0.70\Big)\;.$$

The results can be tabulated as follows.

$z_i \;\backslash\; z_j$	1	2	3	4	5
1	0.10	–0.03	–0.17	–0.30	–0.44
2	–0.13	0.18	0.05	–0.09	–0.22
3	–0.37	–0.05	0.26	0.13	–0.01
4	–0.60	–0.29	0.03	0.34	0.21
5	–0.84	–0.52	–0.21	0.11	0.42

This table shows the preference for similar alters: in all rows, the highest value is at the diagonal ($v_j = v_i$). The ego and alter parameters are close to 0, therefore the similarity effect is dominant. However, note that the formula uses raw values for v_i and v_j but divides the values for the absolute difference $|v_i - v_j|$ by Δ_V which here is $5 - 1 = 4$. Therefore the weight of 0.09 for the alter effect is not completely negligible compared to the weight of 0.90 for the similarity effect. The positive alter effect leads to a preference for ties to alters with a high v_j value which goes against the similarity effect for $v_i = 1$ but strengthens the similarity effect for $v_i = 5$. The table shows that the net resulting preference for similar others is strongest for actors (egos) high on drinking behavior, and weakest for actors in the middle and low range of drinking behavior.

For drug use, the formula yields

$$0.14\,(v_i - \bar{v}) \;-\; 0.13\,(v_j - \bar{v}) \;+\; 0.67\Big(1 \;-\; \frac{|v_i - v_j|}{\Delta_V} \;-\; 0.7533\Big)\;,$$

which leads to the following table.

$z_i \;\backslash\; z_j$	1	2	3	4
1	0.16	–0.19	–0.54	–0.89
2	0.08	0.17	–0.18	–0.53
3	–0.01	0.08	0.17	–0.18
4	–0.10	–0.00	0.09	0.18

In each row the highest value is at the diagonal, which shows that indeed everybody prefers to be friends with similar others also with respect to drug use. The negative alter effect supports this for low v_i values and counteracts it for high v_i values. This is seen in the table in the strong preference of low drug users ($v_i = 1$) for others who are low on drug use, and the very weak preference for high drug users ($v_i = 4$) for others also high on drug use.

An alternative specification uses the drink ego × drink alter interaction together with the drink squared alter effect in the network dynamics model, and similarly for drug use; for the behavior dynamics, an alternative specification uses the average alter effect. This leads to the following table of results.

```
Network Dynamics
 1. rate:  constant network rate (period 1)          8.0978  (   1.5118)
 2. rate:  constant network rate (period 2)          5.7781  (   0.9474)
 3. eval:  outdegree (density)                      -2.1333  (   0.2196)
 4. eval:  reciprocity                               2.3033  (   0.2184)
 5. eval:  transitive ties                           0.2430  (   0.2059)
 6. eval:  number of actors at distance 2           -1.0011  (   0.2275)
 7. eval:  drink alter                               0.1041  (   0.1348)
 8. eval:  drink squared alter                       0.0141  (   0.1329)
 9. eval:  drink ego                                 0.0078  (   0.1157)
10. eval:  drink ego x drink alter                   0.1655  (   0.1095)
11. eval:  drug use alter                           -0.2603  (   0.2436)
12. eval:  drug use squared alter                   -0.0249  (   0.1945)
13. eval:  drug use ego                             -0.0214  (   0.1454)
14. eval:  drug use ego x drug use alter             0.1976  (   0.1146)

Behavior Dynamics
15. rate:  rate drink period 1                       1.3218  (   0.3632)
16. rate:  rate drink period 2                       1.7884  (   0.5053)
17. eval:  behavior drink shape                      0.3820  (   0.2421)
18. eval:  behavior drink average alter              1.1414  (   0.6737)
19. eval:  behavior drink: effect from drink        -0.5428  (   0.2839)
```

For this specification, the formulae in Section 13.1.1 imply that the components in the network objective function corresponding to the effects of variable V are

$$\beta_{\text{ego}}\,(v_i - \bar{v})\,x_{i+} + \beta_{\text{alter}} \sum_j x_{ij}\,(v_j - \bar{v}) + \beta_{\text{sq. alter}} \sum_j x_{ij}\,(v_j - \bar{v})^2 + \beta_{\text{e×a}} \sum_j x_{ij}\,(v_i - \bar{v})\,(v_j - \bar{v})\;. \quad (8)$$

The contribution of the single tie variable x_{ij} to this formula is equal to

$$\beta_{\text{ego}}\,(v_i - \bar{v}) \;+\; \beta_{\text{alter}}\,(v_j - \bar{v}) \;+\; \beta_{\text{sq. alter}}\,(v_j - \bar{v})^2 \;+\; \beta_{\text{e×a}}\,(v_i - \bar{v})\,(v_j - \bar{v})\;. \quad (9)$$

Filling in the estimates for the effects of drinking behavior yields

$$0.01\,(v_i - \bar{v}) \;+\; 0.10\,(v_j - \bar{v}) \;+\; 0.01\,(v_j - \bar{v})^2 \;+\; 0.17(v_i - \bar{v})\,(v_j - \bar{v})\;.$$

and this gives the following table.

v_i \ v_j	1	2	3	4	5
1	0.54	0.27	0.01	–0.23	–0.45
2	0.20	0.09	0.00	–0.07	–0.13
3	–0.15	–0.09	–0.01	0.08	0.19
4	–0.49	–0.26	–0.02	0.24	0.51
5	–0.83	–0.44	–0.03	0.39	0.83

For drug use we obtain the formula

$$-0.02\,(v_i - \bar{v}) \;-\; 0.26\,(v_j - \bar{v}) \;-\; 0.02\,(v_j - \bar{v})^2 \;+\; 0.20(v_i - \bar{v})\,(v_j - \bar{v}) \;.$$

and the following table.

v_i \ v_j	1	2	3	4
1	0.18	–0.18	–0.58	—1.04
2	0.06	–0.10	–0.31	–0.57
3	–0.06	–0.02	–0.03	–0.10
4	–0.18	0.06	0.24	0.38

The fact that we are using three variables involving alter (alter, alter squared, interaction) instead of two (alter and similarity) leads to greater freedom in the curve that is fitted: the top (or, in the rare case of a reversed pattern, bottom) of the attractiveness of alters is not necessarily obtained at the diagonal, i.e., at ego's value. Straightforward calculus shows us that (9) is a quadratic function and obtains its extreme value (a maximum if $\beta_{\text{sq. alter}}$ is negative, a minimum if it is positive – the latter is, in general, less likely) for

$$v_j \;=\; \bar{v} \;-\; \frac{\beta_{\text{alter}} \;+\; \beta_{\text{e×a}}\,(v_i - \bar{v})}{2\,\beta_{\text{sq. alter}}} \;. \tag{10}$$

If the effect $\beta_{\text{sq. alter}}$ of the squared alter's value is negative and the interaction effect $\beta_{\text{e×a}}$ is positive, then this location of the maximum increases with ego's own value, v_i. Of course the number given by (10) will usually not be an integer number, so the actual value of v_j for which attractiveness is maximized is the integer in the range of V closest to (10).

For drinking there is a weak positive effect of squared drinking alter; the effect of squared drug use alter is weak negative. For drinking we see that the most attractive value for egos with $v_i = 1$ or 2 is no drinking, $v_j = 1$, whereas for egos with $v_i \geq 3$ the most attractive alters are those who drink most, $v_j = 5$. We also see that egos with the highest drinking behavior are those who differentiate most strongly depending on the drinking behavior of their potential friends.

For drug use the situation is different. Actors with $v_i = 1$ or 2 prefer friends with drug use $v_j = 1$; for actors with $v_i = 3$ the difference is hardly discernible, but if we consider the differences even though they are tiny, then they are most attracted to others with $v_j = 2$; actors with the highest drug use ($v_i = 4$) differentiate most strongly, and are attracted most to others with also the highest drug use.

The differences between the results with the similarity effects and the interaction effects are minor. The extra degrees of freedom of the latter model gives a slightly closer fit to the data. However, the differences between the two fits are not significant, as can be shown e.g. by score-type tests.

14.1.2 Ego – alter influence tables

In quite a similar way as in the preceding section, from the output tables and the formulae for the effects we can construct tables indicating how attractive various different values of the behavior are, depending on the behavior of the actor's friends.

In the first model, the estimated coefficients in the behavior evaluation function are as follows.

```
15. eval:  behavior drink shape                          0.3618  (   0.1946)
16. eval:  behavior drink average similarity             3.9689  (   2.2053)
17. eval:  behavior drink: effect from drink            -0.0600  (   0.1181)
```

The dependent behavior variable now is indicated Z. (In the preceding section the letter V was used, but this referred to any actor variable predicting network dynamics, whether it was also a dependent variable or not.) The formulae in Section 13.2.1 show that the evaluation function for this model specification is

$$u^{\text{beh}} \;=\; \beta_{\text{trend}}\,(z_i - \bar{z}) \;+\; \beta_{\text{drink}}\,(z_i - \bar{z})^2 \;+\; \beta_{\text{av. sim}}\,\frac{1}{x_{i+}}\,\sum_j x_{ij}(\text{sim}^z_{ij} - \widehat{\text{sim}^z}) \;. \tag{11}$$

In the second model, the table gave the following results.

```
17. eval:  behavior drink shape                          0.3820  (   0.2421)
18. eval:  behavior drink average alter                  1.1414  (   0.6737)
19. eval:  behavior drink: effect from drink            -0.5428  (   0.2839)
```

Here the evaluation function is

$$u^{\text{beh}} \;=\; \beta_{\text{trend}}\,(z_i - \bar{z}) \;+\; \beta_{\text{drink}}\,(z_i - \bar{z})^2 \;+\; \beta_{\text{av. alter}}\,(z_i - \bar{z})(\bar{z}_{(i)} - \bar{z}) \;, \tag{12}$$

where $\bar{z}_{(i)}$ is the average Z value of i's friends[9],

$$\bar{z}_{(i)} = \frac{1}{x_{i+}}\,\sum_j x_{ij}\,z_j \;.$$

Equation (12) is simpler than equation (11), because (12) is a quadratic function of z_i, with coefficients depending on the Z values of i's friends as a function of their average, whereas (11) depends on the entire distribution of the Z values of i's friends.

Suppose that, in model (11), the similarity coefficient $\beta_{\text{av. sim}}$ is positive, and compare two focal actors, i_1 all of whose friends have $z_j = 3$ and i_2 who has four friends, two of whom with $z_j = 2$ and the other two with $z_j = 4$. Both actors are then drawn toward the preferred value of 3; but the difference between drinking behavior 3 on one hand and 2 and 4 on the other hand will be larger for i_1 than for i_2. In model (12), on the other hand, since the average is the same, both actors would be drawn equally strongly toward the average value 3.

For model (11), consider actors in the extreme situation that all their friends have the same behavior z_{ij}. For the parameters given above, the behavior objective function then reads

$$u^{\text{beh}} \;=\; 0.36\,(z_i - \bar{z}) \;-\; 0.06\,(z_i - \bar{z})^2 \;+\; 3.97\,(\text{sim}^z_{ij} - \widehat{\text{sim}^z}) \;.$$

This can be tabulated as follows.

[9] If i has no friends, i.e., $x_{i+} = 0$, then $\bar{z}_{(i)}$ is defined to be equal to $\bar{z}$.

$\bar{z}_{(i)}$ \ z_i	1	2	3	4	5
1	–0.05	–0.82	–1.71	–2.72	–3.84
2	–1.38	0.50	–0.39	–1.39	–2.52
3	–2.70	–0.82	0.94	–0.07	–1.20
4	–4.02	–2.14	–0.39	1.25	0.13
5	–5.35	–3.47	–1.71	–0.07	1.45

For the other model, filling in the estimated parameters in (12) yields

$$u^{\text{beh}} = 0.38\,(z_i - \bar{z}) - 0.54\,(z_i - \bar{z})^2 + 1.14\,(z_i - \bar{z})(\bar{z}_{(i)} - \bar{z}) \ .$$

For a given average Z values of i's friends, this is a quadratic function of z_i. The following table indicates the behavior objective function for z_i (columns) as a function of the average drinking behavior of i's friends (rows).

$\bar{z}_{(i)}$ \ z_i	1	2	3	4	5
1	1.87	1.59	0.22	–2.23	–5.76
2	–0.55	0.32	0.09	–1.22	–3.61
3	–2.96	–0.95	–0.04	–0.20	–1.46
4	–5.37	–2.22	–0.16	0.81	0.70
5	–7.78	–3.49	–0.29	1.82	2.85

We see that, even though the squared function does not necessarily draw the actors toward the average of their friends' behavior, for these parameters the highest values of the behavior objective function are obtained indeed when the focal actor (i) behaves just like the average of his friends. It should be noted that no between-ego comparisons are made, so comparisons are meaningful only within rows. The values far away from the maximum contrast in this case more strongly than in the case of the model with the average similarity effect, but these differences here are not significant.

Another way to look at the behavior objective function is to consider the location of its maximum. This function here can be written also as

$$u^{\text{beh}} = \big(0.38 + 1.14(\bar{z}_{(i)} - \bar{z})\big)\,(z_i - \bar{z}) - 0.54\,(z_i - \bar{z})^2 \ .$$

This function is maximal for

$$z_i = \bar{z} + 0.35 + 1.05\,(z_i - \bar{z}) \ .$$

15 Changes compared to earlier versions

This begins at end October 2009, and only details changes which affect the user. (Programmers should consult the changeLog file on CRAN or in the R-forge repository.)

- 2010-01-28 R-forge revision 48 Fix to bug in sorting effects for multiple dependent variables.
- 2010-01-26 R-forge revision 47 (RSienaTest only)
  - New version: 1.0.10
  - Multiple networks
  - Constraints of higher, disjoint, atLeastOne between pairs of networks.

- 2010-01-19 R-forge revision 45 (RSiena), 46 (RSienaTest)
  New documentation for the effects object.
- 2010-01-18 R-forge revision 43 (RSiena)
  - new behavior effects
  - user specified interactions
  - new utilities to update the effects object
- 2010-01-15 R-forge revision 41 (RSienaTest only)
  - new effect: Popularity Alter, and altered effect1-3 to integers to correct bug in fix(myeff)
  - new utility functions to update effects object
  - no longer necessary to include underlying effects for interactions.
  - user parameter for number of unspecified behavior interactions
  - remove extra sqrt roots in standard error of rates for conditional estimation (see revision 31)
- 2010-01-15 R-forge revision 40: RSiena only
  remove extra sqrt roots in standard error of rates for conditional estimation (see revision 32)
- 2010-01-02 R-forge revision 34
  Corrected layout of print and xtable for SienaFit objects with both behavior and network variables.
- 2010-01-01 R-forge revision 33
  Updated change log and manual in RSiena and changelog in RSienaTest.
- 2010-01-01 R-forge revision 32 print07report.r: corrected standard errors for rate estimate for conditional estimation: needed square roots. RSiena
- 2009-12-31 R-forge revision 31
  - print07report.r: corrected standard errors for rate estimate for conditional estimation: needed square roots. RSienaTest only
  - more behavior effects in RSienaTest.
- 2009-12-17 R-forge revision 30
  Fixed bug in dyadic interactions in RSienaTest
- 2009-12-17 R-forge revision 29
  Fixed bug in 3-way interactions in RSienaTest
- 2009-12-14 R-forge revision 28
  Fixed bug in use of multiple processors for RSiena.
- 2009-12-14 R-forge revision 27
  Fixed bug in use of multiple processors for RSienaTest.

- 2009-12-01 R-forge revision 26

  Created RSienaTest which includes user specified interactions.

- 2009-11-20 R-forge revision 25
  - version number 1.0.8
  - The default method for estimation is conditional if there is only one dependent variable.
  - Movement of behavior variable restricted if all observed changes are in one direction. In this case, linear change effects removed.
  - If all observed changes in a network are in one direction, density effects are removed.
  - If a behavior variable only takes two values the quadratic effects are not selected by default.
  - t-statistics appear on print of sienaFit object.
  - easier to use xtable method
  - warning if behavior variables are not integers
  - Fixed bug in editing all effects in the gui.
  - Fixed a bug in effect creation for changing dyadic covariates
  - Fixed a bug in returning simulated dependent variables
  - Now fails if there are only two waves but you have a changing covariate. In the GUI, can just change the type.
- 2009-11-08 R-forge revision 24
  - version Number 1.0.7
- 2009-11-08 R-forge revision 23
  - corrected bug in creation of effects data frame for multi group projects and for changing covariates
  - added effect numbers to the Estimation screen
- 2009-11-08 R-forge revision 22
  - new option to edit effects for one dependent variable at a time. Model options screen layout altered slightly.
- 2009-11-08 R-forge revision 21
  - Fixed a bug causing crashes (but not on Windows!) due to bad calculation of derivative matrix.
- 2009-10-31 R-forge revision 17
  - version Number 1.0.6
  - xtable method to create LaTeXtables from the estimation results object.
  - added support for bipartite networks
  - structural zeros and 1's processing checked and amended
  - use more sophisticated random number generator unless parallel testing with siena3.

16 References

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